

# **Estimation of Modulus of Elasticity from Mean Grain Size of Granular Soil and Spreadsheet of Settlement Computational Methods**



## **FINAL YEAR PROJECT UG-2014**

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This is to certify that the  
Final Year Project, titled

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Has been accepted towards the requirements

for the undergraduate degree

in

**CIVIL ENGINEERING**

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## **ABSTRACT**

Soil Young's modulus ( $E$ ), commonly referred to as soil elastic modulus, is an elastic soil parameter and a measure of soil stiffness. It is defined as the ratio of the stress along an axis over the strain along that axis in the range of elastic soil behavior. The elastic modulus is often used for estimation of soil settlement and elastic deformation analysis.

Soil elastic modulus can be estimated from laboratory or in-situ tests or based on correlation with other soil properties. In laboratory, it can be determined from tri-axial test or indirectly from odometer test. On field, it can be estimated from Standard penetration test, Cone penetration test, pressure meter or indirectly from dilatometer test.

The main hurdle in estimating the settlement for a desired structure is to identify the value of elastic modulus ( $E$ ). As a lot of work has done for the calculation of elastic modulus but a proper estimation for elastic modulus has yet to achieve.

Our basic aim is to increase our understanding of interaction between elastic modulus and Soil Penetration Test value ( $N$  value), elastic modulus and Cone Penetration Test value ( $q_c$  value). We aim to achieve a relationship between  $D_{50}$  and elastic modulus for general granular soils

We aim to make automated excel spread sheets for various Settlement methods proposed by different geotechnical Scientists and researchers by using elastic modulus of soil and their comparison with settle 3D.

# Table of Contents

ACKNOWLEDGMENTS .....	3
ABSTRACT.....	4
<b>LIST OF FIGURES .....</b>	<b>8</b>
<b>Chapter 1 .....</b>	<b>10</b>
INTRODUCTION .....	10
1.1 BACKGROUND .....	10
1.2 OBJECTIVES AND LIMITATIONS OF STUDY: .....	11
1.3 LEARNING OUTCOMES: .....	12
<b>CHAPTER 2.....</b>	<b>13</b>
LITERATURE REVIEW .....	13
2.1 GENERAL.....	13
2.1.1 FOUNDATION ENGINEERING .....	13
2.1.2 GEOTECHNICAL ENGINEERING.....	13
2.1.3 STRUCTURAL ENGINEERING .....	14
2.1.4 UNCERTAINTIES .....	14
2.2 SETTLEMENT .....	14
2.2.1 COMPONENTS OF SETTLEMENT.....	15
THE COMPONENTS OF SETTLEMENT OF A FOUNDATION ARE:.....	15
2.2.1.1 IMMEDIATE SETTLEMENT .....	15
2.2.1.2 CONSOLIDATION SETTLEMENT .....	15
2.2.1.3 SECONDARY COMPRESSION .....	16
2.2.1.4 SETTLEMENT LIMITS.....	16
2.3 PUBLICATIONS.....	16
2.4 METHODS REVIEWED .....	18
2.4.1 CANADIAN FOUNDATION ENGINEERING MANUAL (1975, 1985, 1992) (CFM).....	18
2.4.2 TSCHEBOTARIOFF (1953, 1971).....	20
2.4.3 CARRIER AND CHRISTIAN (1973).....	22

2.4.4 THOMAS (1968).....	23
2.4.5 D'APPOLONIA ET AL. (1970).....	27
2.4.6 PAPADOPOULOS (1992) .....	27
2.4.7 SCHMERTMANN ET AL. (1978).....	29
2.4.7.1 RECENT MODIFICATIONS IN STRAIN-INFLUENCE FACTOR.....	31
DIAGRAMS .....	31
2.5 STANDARD PENETRATION TEST.....	34
2.6 CONE PENETRATION TEST.....	38
<b>CHAPTER 3.....</b>	<b>44</b>
METHODOLOGY .....	44
3.1 DESIGN CHART METHODOLOGY .....	44
3.1.1 INPUT DATA.....	44
3.1.2 BEARING CAPACITY CALCULATIONS .....	45
3.1.3 SETTLEMENT CALCULATIONS .....	45
3.1.3.1 NON-COHESIVE SOIL.....	45
3.1.3.2 USING AUTOMATED WORKBOOK.....	45
3.1.3.3 CORRELATIONS .....	46
3.1.3.4 CALCULATION OF ELASTIC MODULUS .....	46
3.1.3.5 FRICTION ANGLES OF GENERAL GRANULAR SOILS.....	47
3.1.4 CORRELATION OF ELASTIC MODULUS AND MEAN GRAIN SIZE.....	48
3.1.5 THE TERM W .....	49
3.2 ADDITIONAL FEATURE.....	49
3.2.1 GRADATION CURVE .....	49
3.3 SOIL TEST DATA .....	49
3.4 OUTPUT OF SPREADSHEET .....	50
3.4.1 SETTLEMENT.....	50
3.4.2 ELASTIC MODULUS .....	50
<b>CHAPTER 4.....</b>	<b>51</b>

RESULTS AND DISCUSSIONS.....	51
4.1 DESIGN CHARTS .....	51
4.2 SETTLEMENT SPREAD SHEETS.....	52
4.2.1 HOME PAGE .....	52
4.2.1.1 INPUT SECTION .....	53
4.2.1.2 OUTPUT SECTION .....	55
<b>CHAPTER 5.....</b>	<b>56</b>
VERIFICATION OF RESULTS .....	56
5.1 VERIFICATION USING SETTLE 3D .....	56
5.1.1 EXAMPLE1: SETTLE – 3D (SETTLEMENT).....	56
5.1.2 EXAMPLE 1: SPREAD SHEET (SETTLEMENT).....	57
5.1.3 RESULTS OF EXAMPLE 1 (SETTLEMENT).....	57
5.2 EXAMPLES: ELASTIC MODULUS AND MEAN GRAIN SIZE RELATION.....	57
5.2.1 VERIFICATION OF E & D <sub>50</sub> RELATION.....	58
5.2.1.1 EXAMPLE 1.....	58
5.2.1.2 EXAMPLE 2.....	58
LIMITATIONS AND RECOMMENDATIONS.....	59
REFERENCES .....	60

## LIST OF FIGURES

Figure 1: Chart for influence factor, $I_c$ , after Kany (1959) from Canadian Foundation Manual (1985)	20
Figure 2: Compression of a Truncated Pyramid of Elastic Material	21
Figure 3: Layer Thickness Correction Factor, $C$ , (after Tschebotarioff 1953, 1971)	22
Figure 4: Settlement Ratio Curves Presented by Carrier and Christian (1973).	23
Figure 5 Fox (1948) Embedment Correction Factor.	25
Figure 6: Thomas (1968) Elastic Modulus from CPT	26
Figure 7: Settlement Ratio as a Function of Load Level (Thomas 1968).	26
Figure 8: Papadopoulos (1992) Settlement Factor.	29
Figure 9: Theoretical and experimental distribution of vertical strain influence factor below the center of a footing	30
Figure 10: Revised strain influence factor diagram suggested by Schmertmann et al. (1978)	30
Figure 11 Strain influence diagram suggested by Terzaghi et al. (1996).	32
Figure 12 Variation of $I_z'/I_z$ with $D_f/B$ (after Terzaghi et al. 1996)	33
Figure 13 Correlation between $E_s$ and $q_c$ for square and circularly loaded areas [adapted from Terzaghi et al. (1996)].	34
Figure 14 Comparison of end of construction predicted and measured $S_e$ of foundations on sand and gravel	34
Figure 15 estimate of Soil Modulus from SPT & CPT - comparison	36
Figure 16 Elastic Modulus for SPT Data	37
Figure 17 Elastic Modulus for SPT (continued)	38
Figure 18 Modulus from SPT and CPT (after Bowles 1988)	40
Figure 19 Soil Modulus from CPT (from Mitchell and Gardner)	41
Figure 20 Different Correlations for Calculating Modulus (various)	42



Figure 21 Different Correlations for Calculating Modulus (continued)	43
Figure 22 Correlation of N and phi $\phi$	46
Figure 23 Kulhawy & Mayne (1991) Correlation	47
Figure 24 Proposed Relation between W and Elastic Modulus in tsf	51
Figure 25 General Overview of Home page of Settlement Sheet	52
Figure 26 Data Input Section - Foundation Inputs	53
Figure 27 Data Input Section - Soil Layer Inputs	53
Figure 28 Output Section - Settlement Maximum, Minimum and Comparison Box	55
Figure 29 Output Section - Modulus of Elasticity	55
Figure 30 SETTLE 3d Example Input Data & Settlement Calculated	56
Figure 31 Calculated Settlement on Spreadsheet for the example data	57

## INTRODUCTION

### 1.1 Background

Shallow foundations are among the most intensive applications of principles of basic geotechnical engineering and have served as a reliable, efficient, simple method for load transfer from the super structure to the strata below. Due to the critical nature of their design, the foundations must be rigorously evaluated not only against structural failure and cracking but also against failure due to differential settlement and bearing failure. Due to difficulty in quantizing the exact behavior of soil and the fact that whole interactions of soil particles can never be taken into account when calculating the essential soil strength parameters, the calculated strengths are often estimates based on empirical relationships and statistical models; consequentially a factor of safety of three is mostly applied to account for any over estimation of strength parameter. A controlling bearing capacity estimate (after application of factor of safety) is calculated as the minimum of the bearing capacity estimate provided by the settlement based expression and the expression taking into account the bearing of soil. It has been noted that once the foundation width exceeds 1.5 m, the settlement generally starts controlling the maximum safe bearing capacity.

Settlement being the major factor in designing Foundation of a structure has to be calculated first hand. The most popular methods for settlement predictions, discussed commonly in text books, are the ones proposed by Terzaghi and Peck (1948), Schmertmann (1970), Schmertmann et al. (1978) and Burland and Burbidge (1985). Meyerhof (1956) and Peck and Bazaraa (1969) methods are similar to the one proposed by Terzaghi and Peck (1948). Two of the more recent methods are after Berardi and Lancellotta (1991) and Mayne and Poulos (1999). Sivakugan and Johnson (2004) proposed a probabilistic approach quantifying the uncertainties associated with the settlement prediction methods.

These methods, for the sake of ease of identification can be divided into methods based on the general elastic solution mechanics, the semi empirical methods incorporating factors from

both statistical models as well as mechanical based models as well as completely empirical ones based on data sets obtained from test foundations

In calculating settlement the main controlling factor is to get correct value of elastic modulus of soil. Determining the value of elastic modulus is the most time taking work as its value cannot be calculated directly and various relations have to be used for estimating it. Elastic modulus could also be calculated from in-situ tests but the spread in the results raises questions about the reliability of the dataset as a whole. The correlations between elastic modulus and cone penetration test value ( $E$ ) also have discrepancies such as  $E=2q_c$  to  $3.5q_c$  by Schmertmann (1978) and  $E=11q_c$  by Lambart (1991).

Therefore elastic modulus has very vast ranges and to get an elastic modulus value which is a fair estimate of the strength of soil is as difficult as it is important.

## **1.2 Objectives and Limitations of study:**

Basic aim of project is to provide a correlation generally for elastic modulus of granular soils in term of Mean Grain Size  $D_{50}$  which provides an acceptable value of elastic modulus. By using the values of elastic modulus we can get appropriate settlement as settlement is very critical factor in foundation design.

Since foundations provide basis for every civil engineering structure, so it is important to learn about various methods that are available to get settlement of foundations. This project then aims to study the limitations and assumptions of each method and get a practical idea of where to apply a certain method. The limitations of the project are that not all the methods for calculating settlement are catered in this project. The methods based on standard penetration test and Cone penetration tests were used to make excel sheets. Only granular soils were catered. Elastic behavior was assumed. A selective representative list of relations was used for computing modulus of elasticity

### **1.3 Learning Outcomes:**

Developed a keen insight about

1. Variation of elastic modulus of soil and the effect on the ranges of elastic modulus with the variation of soil.
2. Learned different Settlement computational methods.
3. Developed an acceptable and comprehensive correlation between mean grain size ( $D_{50}$ ) and elastic modulus of soil.
4. Learned how to use computer software for predicting and analyzing settlement using settle 3D.
5. Learned how to use advanced Microsoft excel (MS EXCEL).

## **CHAPTER 2**

### **LITERATURE REVIEW**

#### **2.1 General**

“A structure is no stronger than its connections” although this statement usually invokes images of connections between individual structural members it also applies to those between a structure and the terrain that supports it. These connections are known as its foundations. Even the ancient builders knew that the most carefully designed structure can fail if they are not supported on suitable foundations for example tower of Pisa in Italy is perfect example.

##### **2.1.1 Foundation Engineering**

Foundation engineer should have the knowledge of all the multiple disciplines of Civil Engineering i-e,

1. Geotechnical Engineering
2. Structural Engineering

##### **2.1.2 Geotechnical engineering**

All foundations interact with the ground, so the design must reflect the technical characteristics and behavior of the soil and adjacent rocks, so the engineer has to understand geotechnical engineering, and most civil engineers are also geotechnical engineers.

### **2.1.3 Structural Engineering**

The factors that must be considered in the design of the foundation include; the transfer of the load to the ground and support for the structure. A foundation is a structural element that transmits the load acting on the ground. So whoever can transfer the imposed burdens must understand the principles and practices of building construction. In addition, the foundation supports a structure. We have to understand the sources and the nature of the structural burdens and the tolerance of the movements of the founding structure.

### **2.1.4 Uncertainties**

"Despite much progress in the theory of foundation engineering, there are still gaps in understanding. In general, uncertainties are the result of our limited knowledge of soil conditions." The prediction of the compaction of granular soils is also very uncertain because the location of the modulus of elasticity of the granular soil that are difficult to calculate depend on there being many relationships and correlations for modulus of elasticity and soil penetration (number of shots per foot) and test of cone penetration ( $q_c$  value).

## **2.2 Settlement**

A soil shear failure can result in excessive building deformation and even collapse. Excessive settling can result in structural damage to a building frame nuisances such as sticking doors and windows, cracks in tile and plaster, and excessive wear or equipment failure from misalignment resulting from foundation settlements.

It is necessary to investigate both base shear resistance (ultimate bearing capacity) and settlements for any structure. In many cases settlement criteria will control the allowable bearing capacity.

Except for occasional happy coincidences, soil settlement computations are only best estimates of the deformation to expect when a load is applied.

## 2.2.1 Components of Settlement

The components of settlement of a foundation are:

1. Immediate settlement
2. Consolidation Settlement, and
3. Secondary compression (creep)

$$\Delta H = \Delta H_i + U \Delta H_c + \Delta H_s$$

$\Delta H$  = total settlement,  $\Delta H_c$  = consolidation settlement,  $\Delta H_s$  = secondary compression,  $U$  = average degree of consolidation. Generally, the final settlement of a foundation is of interest and  $U$  is considered equal to 1 (i.e. 100% consolidation).

### 2.2.1.1 Immediate Settlement

Immediate settlement takes place as the load is applied or within a time period of about 7 days. Predominates in cohesion-less soils and unsaturated clay. Immediate settlement analysis are used for all fine-grained soils including silts and clays with a degree of saturation  $< 90\%$  and for all coarse grained soils with large co-efficient of permeability (say above 10.2 m/s)

### 2.2.1.2 Consolidation Settlement

Consolidation settlements are time dependent and take months to years to develop. The leaning tower of Pisa in Italy has been undergoing consolidation settlement for over 700 years. The lean is caused by consolidation settlement being greater on one side. This, however, is an extreme case. The principal settlements for most projects occur in 3 to 10 years.

Dominates in saturated/nearly saturated fine grained soils where consolidation theory applies. Here we are interested to estimate both consolidation settlement and how long a time it will take or most of the settlement to occur.

### **2.2.1.3 Secondary Compression**

Creep occurs under constant effective stress due to continuous rearrangement of clay particles into a more stable configuration.

Creep predominately occurs in highly plastic clays and organic clays.

### **2.2.1.4 Settlement Limits**

Total settlement is the magnitude of downward movement. Differential settlement is non-uniform settlement. It is "the difference of settlement between various locations of the structure. Angular distortion between two points under a structure is equal, to the differential settlement between the points divided by the distance between them.

Theoretically, no damage will be done to a structure if it settles uniformly as a whole regardless of how large the settlement may be. The only damage would be to the connections of the underground utility lines. However, when the settlement is non-uniform (differential), as is always the case, damage may be caused to the structure.

The tolerable, settlements of different structures, vary considerably. Simple-span frames can take considerably greater distortion than rigid frames. A fixed-end arch would suffer greatly if the abutments settle or rotate. For road embankments, storage silos and tanks a settlement of 300mm - 600mm may be acceptable, but for machine foundations the settlement may be limited to 5mm 30mm. Different types of construction materials can withstand different degrees of distortion. For example, sheet metal wall panels do not show distress as readily as brick masonry. In Sands maximum total settlement = 40 mm for isolated footings = 40 to 65 mm for rafts .Maximum differential settlement between adjacent columns = 25 mm.

## **2.3 Publications**

A representative list of literature referred to for the purpose of this project from where these methods were taken are listed below



- SETTLEMENT OF SHALLOW FOUNDATIONS ON GRANULAR SOILS Final Report Alan .lutenegger & Don j. Degroot
- ELASTIC SETTLEMENT OF SHALLOW FOUNDATION ON GRANULAR SOIL- A CRITICAL REVIEW by Braja. M. Das
- SETTLEMENT OF SHALLOW FOUNDATIONS ON GRANULAR SOILS: AN OVERVIEW by Sivkugan (2016)
- CORRELATION OF STANDARD AND CONE PENETRATION TESTS FOR SANDY AND SILTY SAND TO SANDY SILT SOIL Bashar Tarawneh Ph. D, P.E Assistant Professor Civil Engineering Department The University of Jordan Amman, Jordan 11942
- A UNIFIED CPT-SPT CORRELATION FOR NON-CRUSHABLE AND CRUSHABLE AND COHESION LESS SOILS Sayed M. Ahmad a, Sherif W. Agaiby, Ahmed H. Abdel-Rahman

Generally these publications divide soil settlement methods into two different types; Theoretical elasticity based methods that compute layer strain and general empirical, semi empirical and/or statistical methods based on direct field measurement inputs.

While rigorous computation based methodology has been developed in later years to cater for the elastoplastic behavior of soil, the bulk of settlement computational methods treat soil under stress as an elastic medium. These methods generally employ a solution of the form  $s = qB/E$ . The major variation in different methods is the calculation of a dimensionless influence factor that dictates to what extent would each substratum layer receive the increase in stress, and to what extent that load would produce vertical strains and to what extent would those strains contribute to total settlement. Varying from simpler computations like Tschebatarioff and Canadian Foundation Manual to more rigorous strain based computations like Das, Bowles, Whals and Gupta's and Oweiss's methods which calculate different factors to further estimate the value of influence factor I.

The other kind of calculations incorporates empirical, semi-empirical and/or statistical approach based on the regression analysis of large sets of data from settlements on test foundations and on plate load tests on river sands. These methods incorporate field measurements such as blow counts for Soil Penetration Test and Cone tip resistance for Cone

Penetration Test along with correction factors to estimate settlement and range from simpler methods such as Terzaghi, Peck and Mesri to multi-layered methods that incorporate elements from bearing capacity design of foundations such as Stroud's and Hough's methods.

## **2.4 Methods Reviewed**

In this project the main focus is on the immediate settlement of granular soils and the correlation of the mean grain size ( $D_{50}$ ) and elastic modulus of soil. The methods which were reviewed and used during the project for calculating the immediate settlement and making automated Microsoft excel sheet are as follows

1. Canadian Foundation Engineering Manual (1975, 1985, 1992) (CFM)
2. Tschebotarioff (1953, 1971)
3. Carrier and Christian (1973)
4. Thomas (1968)
5. D'Appolonia et al. (1970)
6. Papadopoulos (1992)
7. Schmertmann et al.(1978)
8. Schmertmann (1970)
9. Terzaghi Peck & Misri (1996)
10. Lee & Salgado (2008)

### **2.4.1 Canadian Foundation Engineering Manual (1975, 1985, 1992) (CFM)**

Canadian Foundation Manual often referred to as CFM calculates the settlement by dividing the soil into layers and using a pre-determined value of elastic modulus with a correction factor and the general elastic solution to calculate settlement such:

$$E_i = q_i / E_{\text{soil}}$$

where:

$q_i$  = stress at the  $i$ th layer

$E_{\text{soil}}$  = Soil modulus of elasticity

The total settlement is obtained from:

$$s = \sum E_i \cdot h_i,$$

or

$$s = \sum (q_i / E_s) h_i$$

where:

$s$  = settlement

$h_i$  = thickness of the  $i$ th layer

CFM also presented the equation as a recommendation as:

$$s = (q \cdot B \cdot I_c) / E_s$$

where:

$s$  = settlement

$q_0$  = applied net footing stress

$B$  = footing width

$E_z$  = apparent modulus elasticity

$I_c$  = influence factor settlement of each layer.

The  $I_c$  influence factor was reproduced from Kanye (1959) and like other similar factors incorporates changes and variations in foundation geometry and types among other factors.

The factor is reproduced on the next page and includes different lines for variation in  $L/B$  and  $Z/B$  on y axis

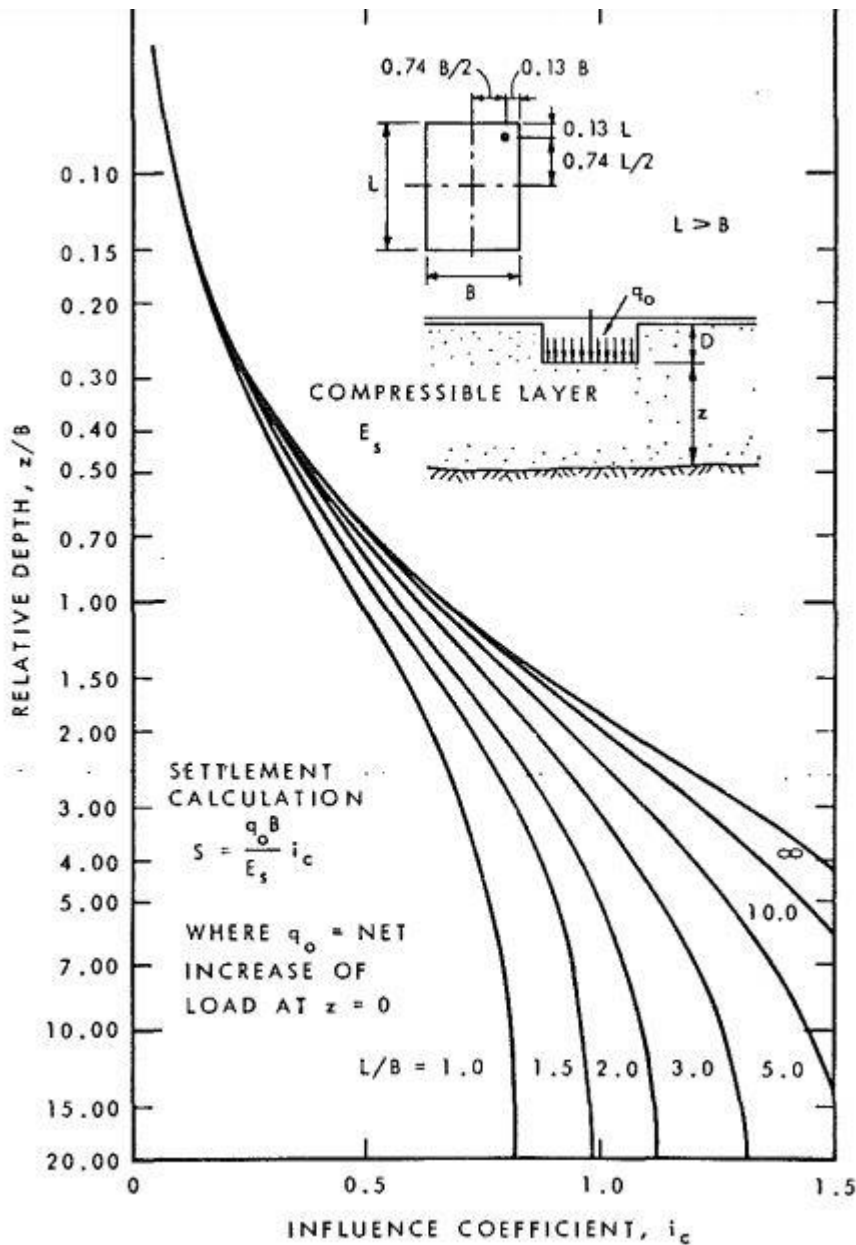


Figure 1: Chart for influence factor,  $I_c$ , after Kany (1959) from Canadian Foundation Manual (1985)

## 2.4.2 Tschebotarioff (1953, 1971)

Tschebotarioff (1953, 1971) suggested a simplified method which works on the assumption that the stresses applied to the soil vertically propagate in a pyramid formation and that each layer will have its own stress share of the pyramid; the individual settlement of each layer can be summed up to produce the total settlement that will occur as a result of application of loading. The method assumes that the area occupation by each layer is  $A = (b + 2H \tan \phi)^2$ ,

where  $\alpha$  is defined as shown in Figure 2. For an assumed value of  $\phi = 30'$ , the method provides a reduced expression for computing settlement as:

$$s = (0.867 q \cdot b \cdot C_s) / E$$

where:

$q$  = applied footing stress

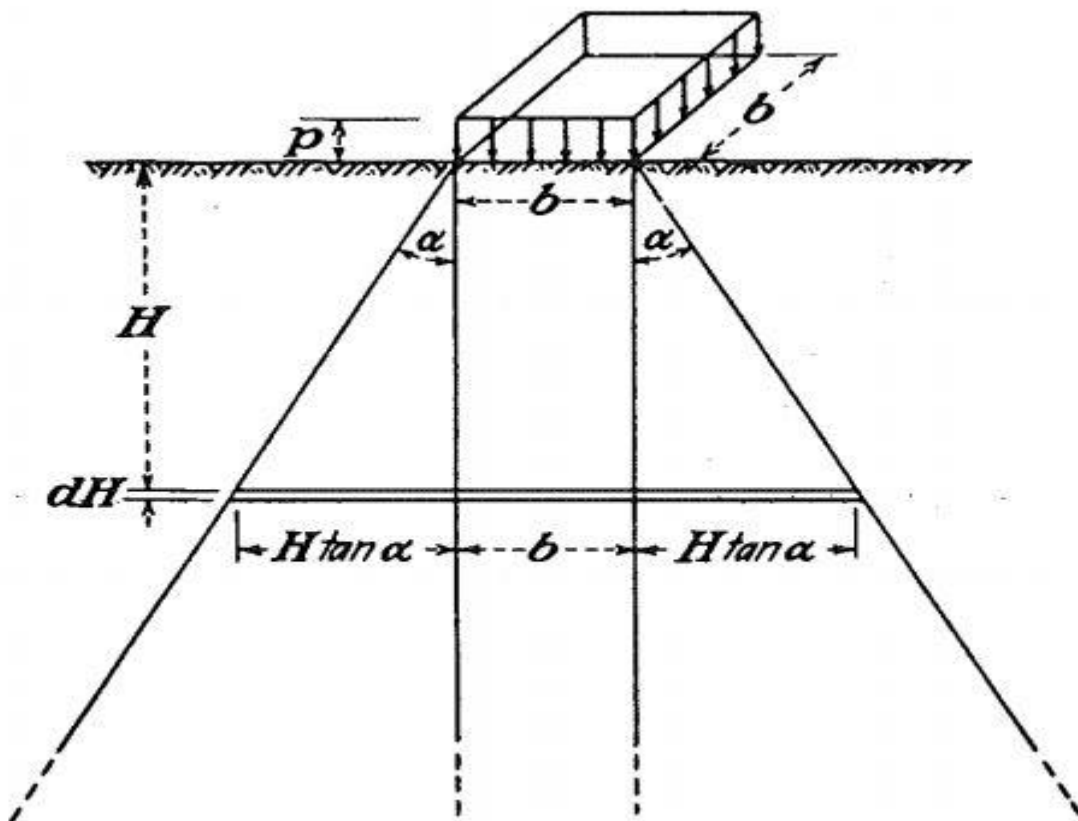
$b$  = footing width

$C_s$  = layer thickness correction factor

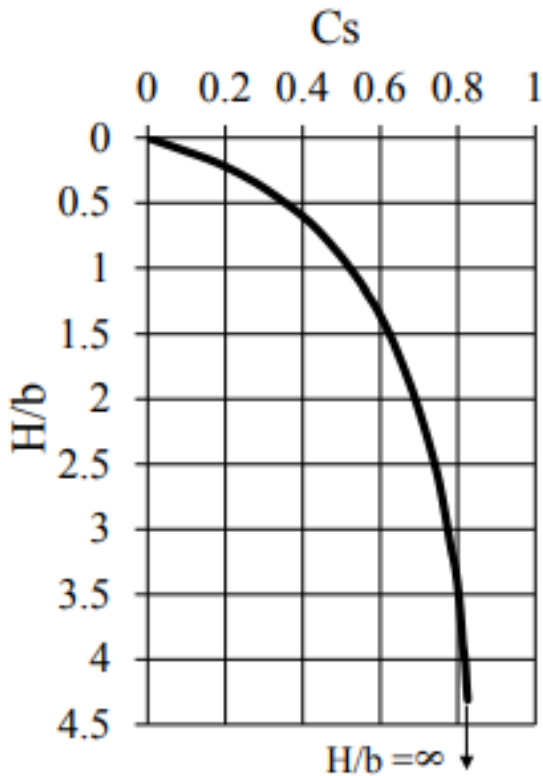
$E$  = Young's Modulus

The correction factor, while catering for changes in foundation geometry and embedment, also caters for increasing values of  $H$ , as with increase in  $H$ , increases the area under the “pyramid” leading to a higher value of Predicted  $Q$

$$s = [(2.0 \cdot q \cdot b) / E] \cdot \log [1 + (1.154 \cdot H) / b]$$



**Figure 2: Compression of a Truncated Pyramid of Elastic Material**



**Figure 3: Layer Thickness Correction Factor, C, (after Tschebotarioff 1953, 1971)**

### **2.4.3 Carrier and Christian (1973)**

Carrier and Christian (1973) used the finite element approach to solve the dislocation and stresses induced by a rigid circular plate resting on an inhomogeneous elastic half space defined by a Young's modulus ( $E$ ) of increasing depth increases with:

$$E = E_0 + Kz$$

where:

$E_0$  = Young's modulus at surface (i.e.,  $z = 0$ )

$K$  = rate of increase in  $E$  with depth

The results of comparison with methods that treat  $E$  as non-varying with depth were presented by considering the elastic settlement ratio as a function of foundation width, similar to what had previously been presented by Terzaghi and Peck (1948, 1967) and Bjerrum and Eggstad (1963). As shown in Figure 4, solutions were shown for various ratios of  $E/K$

ranging from 0 to infinity. These results show that the settlement ratio of footings on a non-homogenous half-space increases linearly with the logarithm of footing width.

An alternative approach may be to use the results of penetration tests, such as the CPT or SPT to evaluate the variation in soil modulus with depth to obtain the value of K. The value of  $E_0$  would then be obtained, as before, using a plate load test on a 0.3m (1ft.) wide plate.

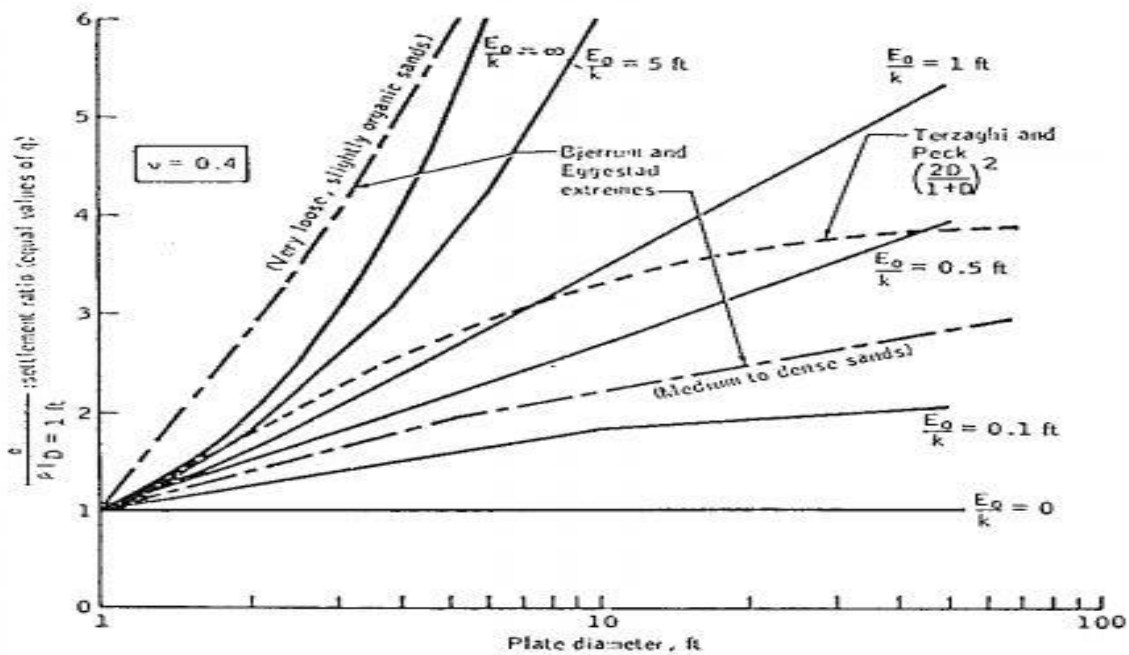


Figure 4: Settlement Ratio Curves Presented by Carrier and Christian (1973).

### 2.4.4 Thomas (1968)

Thomas (1968) suggested a method based essentially on the calculation of consolidation settlements using an expression identical to that of DeBeer and Martens (1957). However, whereas the previous suggestion of DeBeer and Martens (1957) had been to define the constant of compressibility C as:

$$c = 1.5 q/p'_o$$

which can also be used to express the elastic modulus of the soil as:

$$E = 1.5 * q_c$$

Thomas found that for a normally consolidated sand, the elastic modulus was related to cone tip resistance as  $3q < E < 12q$  with the lower coefficient corresponding to high cone tip resistance and grain crushing.

The elastic expression of Section 4 was used to calculate settlements as:

$$s = I * q * B * (1 - \mu^2) / E$$

where:

s = settlement (in ft.)

I = an influence factor which depends on footing geometry (LIB)

q = applied footing stress (in tsf)

B = footing width (in ft)

E = Elastic modulus (in tsf)

$\mu$  = Poisson's ratio

The influence factor, I, incorporating correction for embedment was obtained using the expressions proposed by Fox (1948; see Figure 5).

Thomas (1968) found that the ratio of estimated to observed settlement, defined as  $R_s$ , was related to the level of loading, defined as a percentage of the ultimate bearing capacity as  $q/B$  ( $q$ ) as shown in Figure 7. Schmertmann (1969) pointed out that this method tends to seriously underestimate settlement.



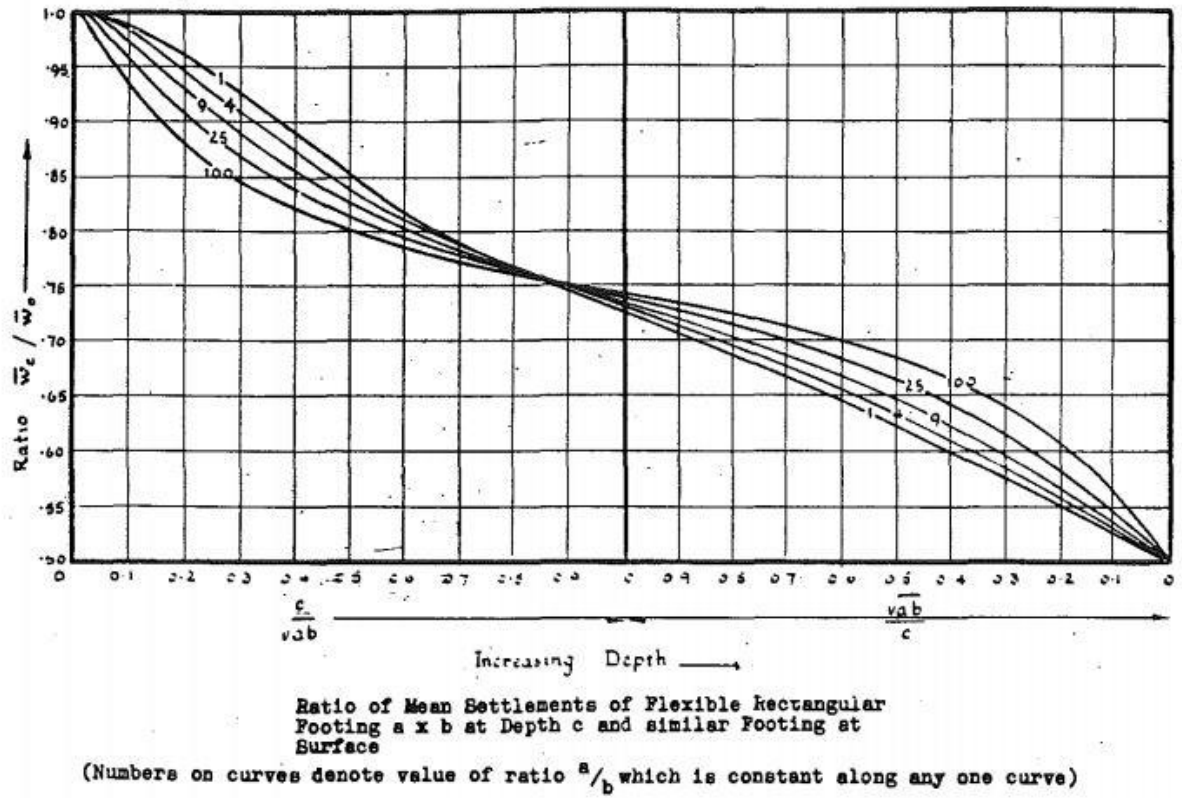


Figure 5 Fox (1948) Embedment Correction Factor.

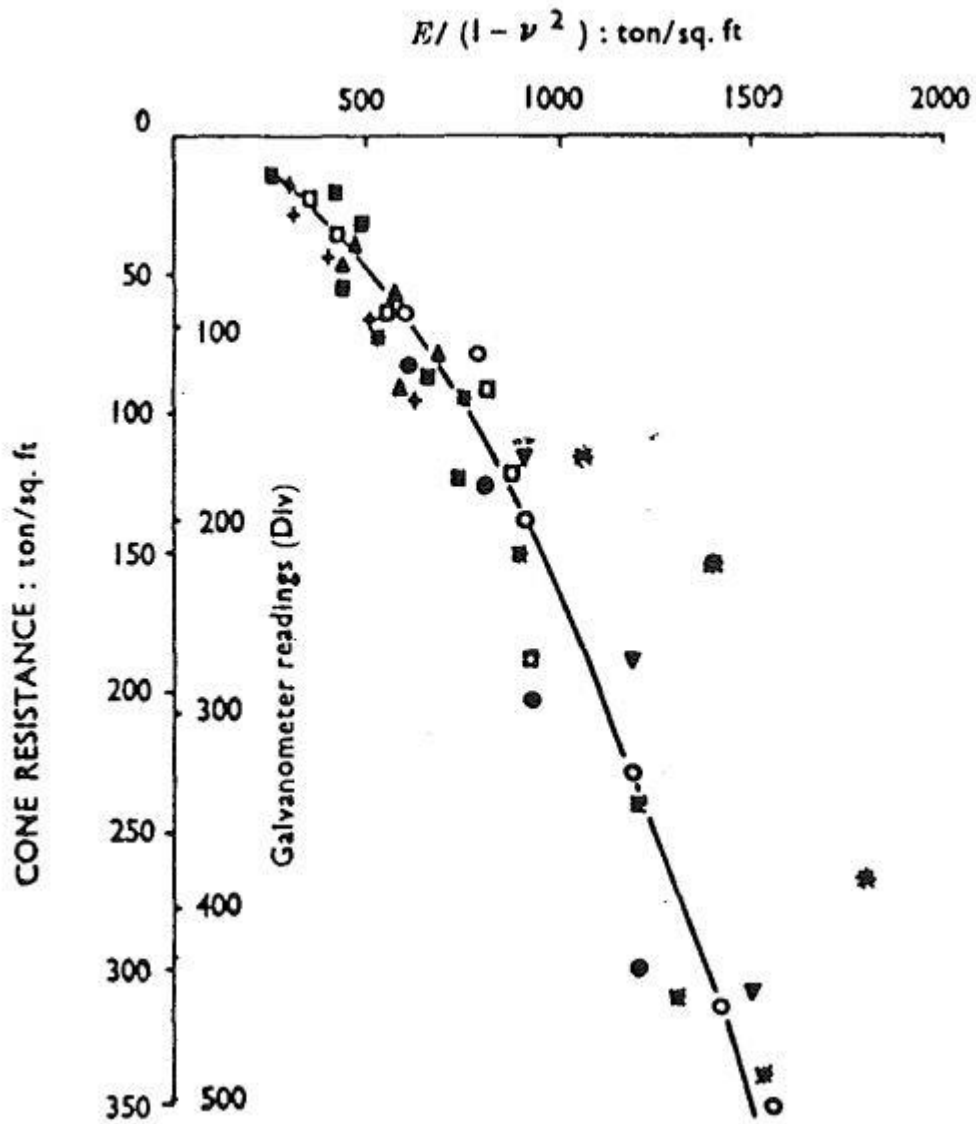


Figure 6: Thomas (1968) Elastic Modulus from CPT

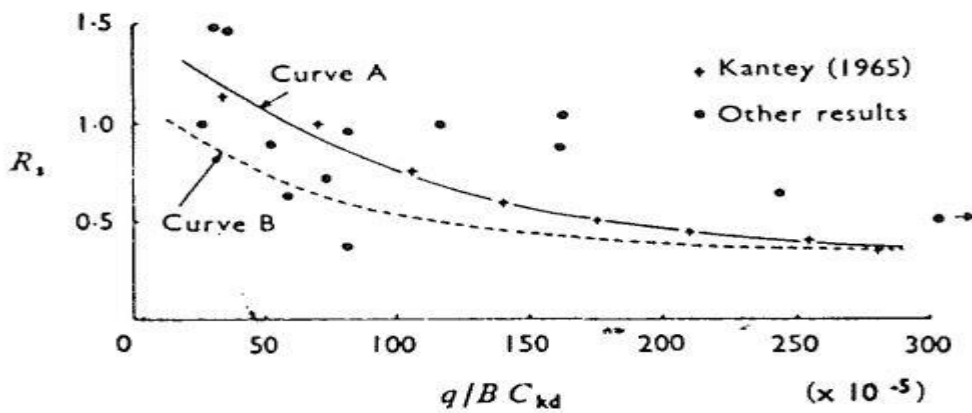


Figure 7: Settlement Ratio as a Function of Load Level (Thomas 1968).

### **2.4.5 D'Appolonia et al. (1970)**

In an extensive study of the settlement performance of a large number of footings on sand, D'Appolonia et al. (1968) used a modification of the Terzaghi and Peck (1948, 1967) and Meyerhof (1956, 1965) methods to predict settlement.

Based on their observations, they suggested that settlement should be estimated as:

$$s = [16 \cdot q / (3N_c)] \cdot C_d$$

$$s = (8 \cdot q / N_c) \cdot [B / (B + 1)]^2 \cdot C_d$$

$$s = (8q / N_c) \cdot C_d$$

where:

s = settlement (in inches)

q = footing stress (in tst)

B = footing width (in ft.)

N<sub>c</sub> = corrected blowcounts

C<sub>d</sub> = embedment correction = 1 - 0.25 (D/B)

### **2.4.6 Papadopoulos (1992)**

Papadopoulos (1992) suggested a method of estimating the settlement of footings resting on granular soils of the elastic solution type as:

s = settlement

q = foundation stress

B = width of a rectangular foundation

E<sub>c</sub> = constrained modulus of the soil for the appropriate stress range

f = a dimensionless factor which depends on soil stress history, geometry, loading and the relation between constrained modulus and effective stress.

According to Papadopoulos (1992) the settlement factor,  $f$  is related to the geometry of the foundation (depth and dimensions), the stress history of the soil, the foundation loading, and the relation between the constrained modulus and the effective stress,  $\sigma'$  as shown in Figure 4.18. The influence of history of applied stresses in soil and other miscellaneous effecting factors were statistically compiled into a factor  $\alpha$  such as:

$$\alpha = q / (y' * B)$$

is indicated in Figure 8.

The constrained modulus,  $E_s$  is related to the effective stress for stresses  $\sigma' = 600$  kPa by a linear expression:

$$E_s = E_0 + \lambda \cdot \sigma' \text{ where:}$$

$E_0$  = constrained modulus for zero effective stress

$\lambda$  = the rate of  $E_s$  increase with stress.

Due to difficulty in calculating the value of gamma. The following expressions for estimating soil modulus were suggested by Papadopoulos:

$$E = 2.5 * q_c \quad (\text{for CPT results})$$

$$E = 7.5 + 0.8N \text{ (MPa)} \quad (\text{for SPT results})$$

A comparison between the settlements predicted using this method and settlement observations showed that in more than 90% of the cases the deviation of the estimated settlement from the measured settlement was  $\pm 50\%$ . Hence the reliability of this method remains low.

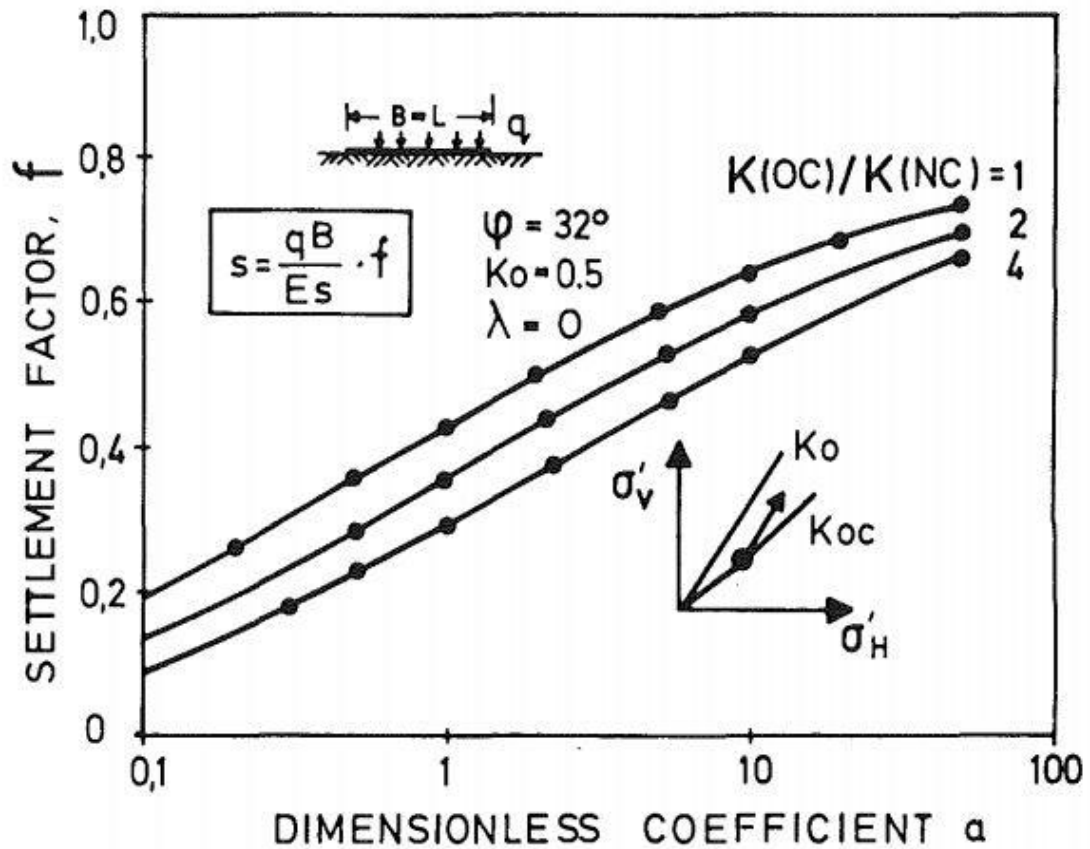


Figure 8: Papadopoulos (1992) Settlement Factor.

### 2.4.7 Schmertmann et al. (1978)

Schmertmann et al. (1978) modified the strain influence factor variation ( $2B-0.6L_z$ ) shown in Figure 9. The revised distribution is shown in Figure 10 for use in equations

According to this, for square or circular foundation:

$$I_z = 0.1 \text{ at } z = 0$$

$$I_z \text{ (peak) at } z = z_p = 0.5B$$

$$I_z = 0 \text{ at } z = z_o = 2B$$

For foundation with  $L/B \geq 10$ :

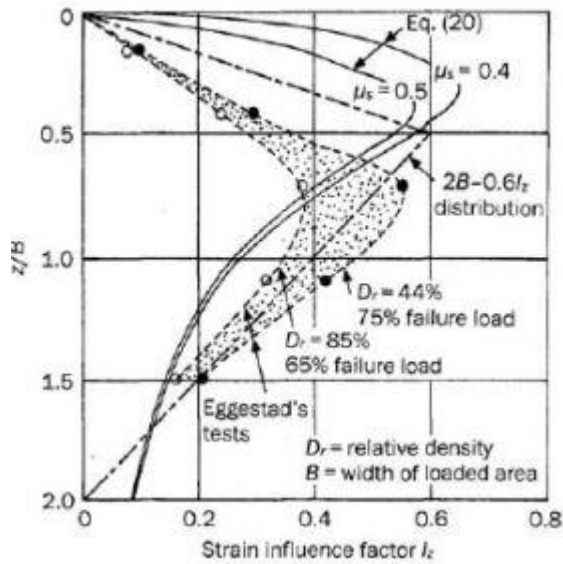
$$I_z = 0.2 \text{ at } z = 0$$

$I_z$  (peak) at  $z = z_p = B$

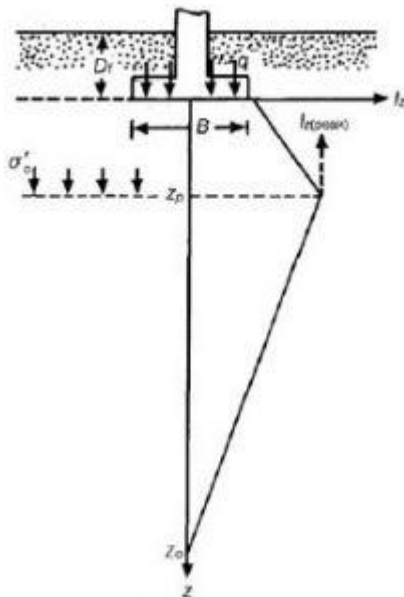
$I_z = 0$  at  $z = z_o = 4B$

where  $L$  = length of foundation. For  $L/B$  between 1 and 10, interpolation can be done. Also

$$I_z \text{ (peak)} = 0.5 + 0.1 * (q/\sigma'_o)^{0.5}$$



**Figure 9: Theoretical and experimental distribution of vertical strain influence factor below the center of a footing**



**Figure 10: Revised strain influence factor diagram suggested by Schmertmann et al. (1978)**

The value of  $\sigma'_o$  is the effective overburden pressure at a depth where  $I_z(\text{peak})$  occurs. Salgado (2008) gave the following interpolation for  $I_z$  at  $z = 0$ ,  $z_p$ , and  $z_o$  for  $L/B = 1$  to  $L/B \geq 10$ .

$$I_z(\text{at } z=0) = 0.1 + 0.0111 \cdot (L/B)^{0.2}$$

$$Z_p/B = 0.5 + 0.0555 \cdot (L/B - 1) \leq 1$$

$$Z_o/B = 2 + 0.222 \cdot (L/B - 1) \leq 4$$

Schmertmann et al. (1978) recommended that.

$$E_s = 2.5 \cdot q_c \text{ (for square and circular foundations)}$$

And

$$E_s = 3.5 \cdot q_c$$

With the modified strain-influence factor diagram,

$$S_e = C_1 \cdot C_2 \cdot q \cdot \sum I_z / E_s \Delta z$$

### **2.4.7.1 RECENT MODIFICATIONS IN STRAIN-INFLUENCE FACTOR**

#### **DIAGRAMS**

More recently some modifications have been proposed to the strain-influence factor diagram suggested by Schmertmann et al. (1978).

Modification Suggested by Terzaghi, Peck and Mesri (1996)

The modification suggested by Terzaghi et al. (1996) is shown in Figure 10.

For this case, for surface foundation condition (that is,  $D_f/B = 0$ )

$$I_z = 0.2 \text{ at } z = 0$$

$$I_z = I_z(\text{peak}) = 0.6 \text{ at } z = z_p = 0.5B$$

$$I_z = 0 \text{ at } z = z_o$$

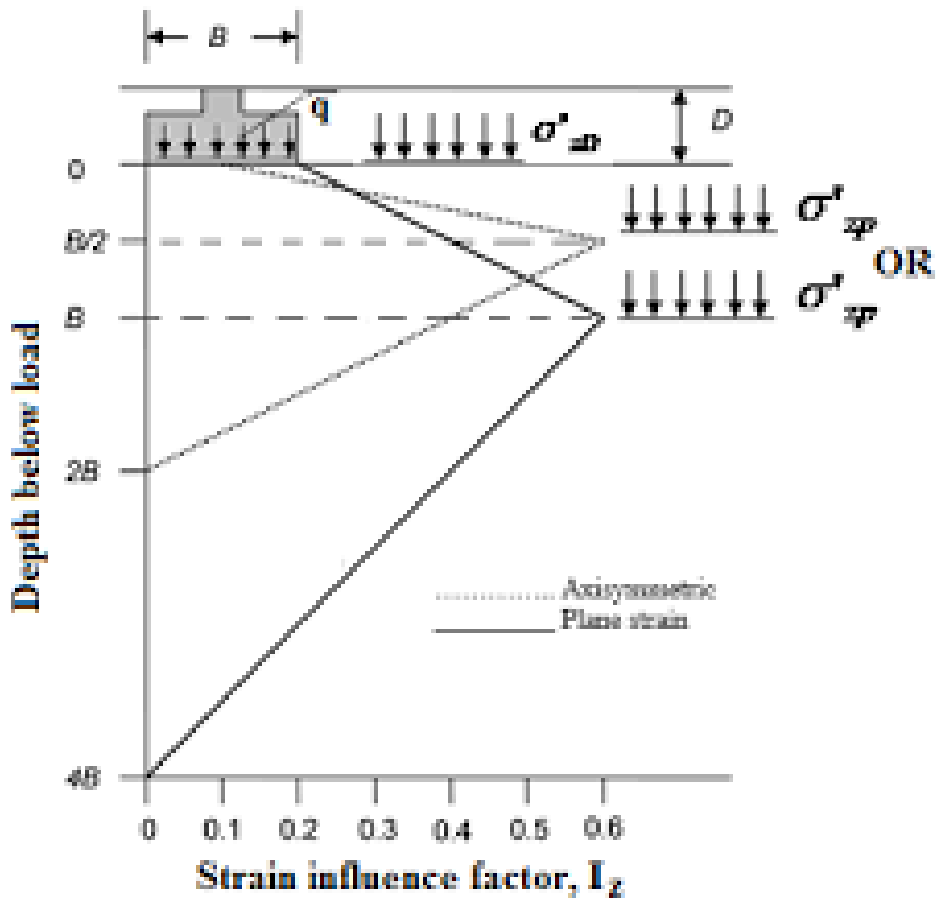


Figure 11 Strain influence diagram suggested by Terzaghi et al. (1996).

$$Z_p = 2[1 + \log(L/B)] \leq 4$$

For  $D_f/B > 0$ ,  $I_z$  should be modified to  $I_z'$ . Figure 12 shows the variation of  $I_z' / I_z$  with  $D_f/B$ .

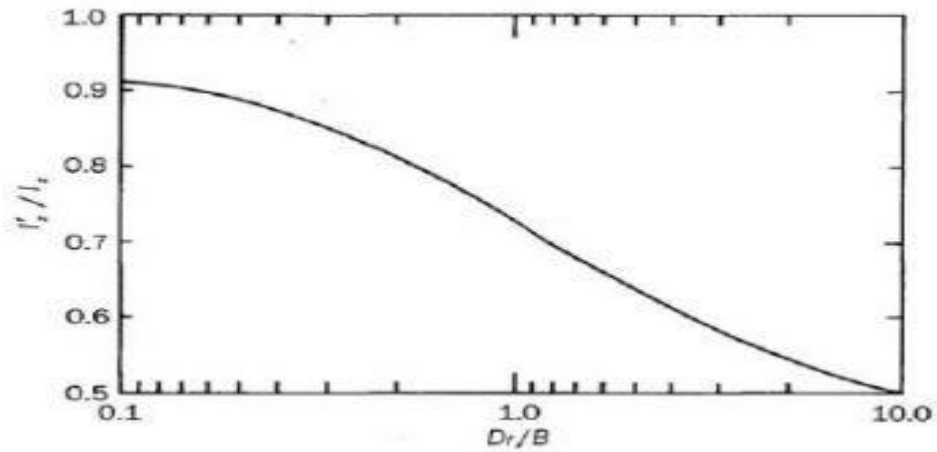
The end of construction settlement can be estimated as

$$S_e = q \sum I_z / E_s \Delta z$$

The settlement due to creep can be calculated as

$$S_{(creep)} = (0.1/q_c) * Z_p * \log(t(\text{days})/1\text{day})$$





**Figure 12 Variation of  $I_z'/I_z$  with  $D_r/B$  (after Terzaghi et al. 1996)**

Where

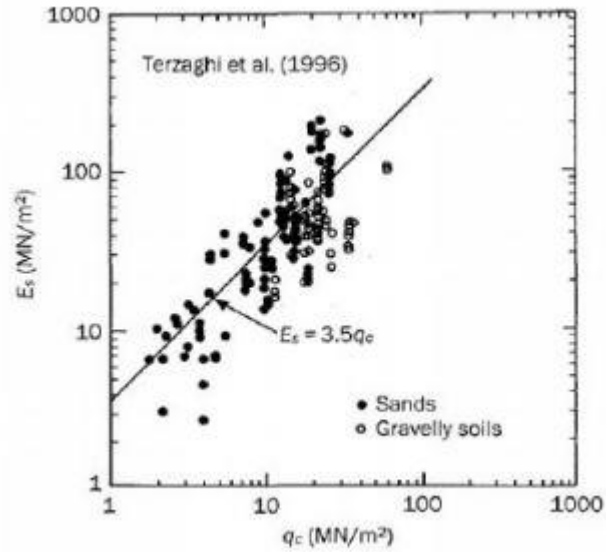
$q_c$  = weighted mean value of measured  $q_c$  values of sub layers between  $z = 0$  and  $z = z_0$  (MN/m<sup>2</sup>).

It has also been suggested that

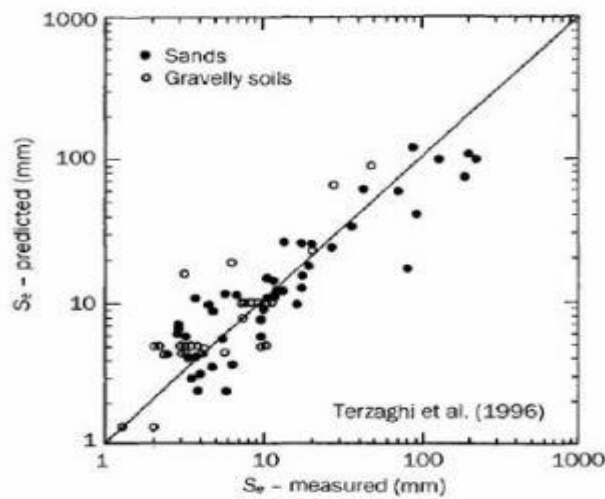
$$E_{s(L/B)}/E_{s(L/B=1)} = 1 + 0.4 \cdot \log(L/B) \leq 1.4$$

where

$$E_{s(L/B)} = q_c \cdot 3.5$$



**Figure 13** Correlation between  $E_s$  and  $q_c$  for square and circularly loaded areas [adapted from Terzaghi et al. (1996)].



**Figure 14** Comparison of end of construction predicted and measured  $S_e$  of foundations on sand and gravel

## 2.5 Standard Penetration Test

Numerous suggestions have been made to use the SPT for estimating the elastic modulus of granular soils (e.g., Schultze and Menzenbach 1961; Schultze and Melzer 1965, etc). Most of these correlations have the form of:

$$E = a \cdot (N + b)$$

where:

E = soil modulus

N = blow counts

a and b = constants (empirical factors)

Alternatively, other forms have been used. In addition to the correlations presented in Tables 4.2 and 4.3, a number of other suggestions have been made. These are summarized in Table 4.4.

Other attempts have been made to correlate the results of the SPT to the constrained modulus of the soil (M) as a function of overburden stress (e.g., Schultze and Melzer 1965). D'Appolonia et al. (1970) suggested correlations between M and SPT blow count N recognizing the influence of stress history. These correlations are presented in the next section of this report and are subsequently shown in Figure 5.7.

Since the constrained modulus, M, is related to the elastic Young's modulus, E, as:

$$M = [E(1-\mu)] / [(1+\mu)(1-2\mu)]$$

an estimate of Poisson's ratio is required to estimate E from M. For most granular soils in drained loading conditions, the constrained modulus probably varies in the range of  $1.2E_s$  to  $1.5E_s$ .

Unfortunately, the realization must be made that there is considerable scatter in suggested correlations between E or M and SPT blowcount N. This should in fact be not altogether unexpected since there is a considerable scatter in SPT results, even at a single site, because of large variations in test procedures that may occur. Additionally, since the source of correlations between modulus and N is highly variable and includes laboratory tests on reconstituted samples, results of field plate tests and results of settlement observations from full scale structures, the correlations will have implicit variability just because of differences in assumptions made. Additionally; since the modulus is strain level dependent, the correlations include comparisons at a range of strain levels.

The various relations between Standard Penetration Test blow counts and soil modulus are shown in the following tables:

**Table 4.2 Estimates of Soil Modulus from SPT and CPT (after Bowles 1988).**

Soil	SPT	CPT
Sand (normally consolidated)	$E_s = 500(N + 15)$ $E_s = (15000 \text{ to } 22000) \ln N$ $E_s^{\S} = (3500 \text{ to } 50000) \log N$	$E_s = 2 \text{ to } 4q_c$ $E_s^{\dagger} = (1 + D_r^2)q_c$
Sand (saturated)	$E_s = 250(N + 15)$	
Sand (overconsolidated)	$E_s^{\ddagger} = 18000 + 750N$ $E_{s(OCR)} = E_{s(nc)} (OCR)^{1/2}$	$E_s = 6 \text{ to } 30q_c$
Gravelly sand and gravel	$E_s = 1200(N + 6)$ $E_s = 600(N + 6) \quad N \leq 15$ $E_s = 600(N + 6) + 2000 \quad N > 15$	
Clayey sand	$E_s = 320(N + 15)$	$E_s = 3 \text{ to } 6q_c$
Silty sand	$E_s = 300(N + 6)$	$E_s = 1 \text{ to } 2q_c$
Soft clay	-----	$E_s = 3 \text{ to } 8q_c$

Notes:

$E_s$  in kPa for SPT and units of  $q_c$  for CPT; divide kPa by 50 to obtain ksf.

N values should be estimated as  $N_{55}$  and not  $N_{70}$

$\dagger$  Vesic' (1970)

$\ddagger$  Author's equation from plot of D'Appolonia et al. (1970).

$\S$  USSR (and may not be standard blowcount N).

**Figure 15 estimate of Soil Modulus from SPT & CPT - comparison**

**Table 4.3 Soil Modulus from Standard Penetration Resistance  
(modified from Mitchell and Gardner 1975)**

Reference	Relationship	Soil Types	Basis	Remarks
Schultze and Melzer (1965)	$E_s = Na_{0.522} \text{ kg/cm}^2$	Dry sand	Penetration tests in field and in test shaft. Compressibility based on $e$ , $e_{max}$ , and $e_{min}$ . (Schulzte and Moussa, 1961)	Correlation Coefficient = 0.730 for 77 tests
Webb (1969)	$E_s = 5(N+15) \text{ tons/ft}^2$ $E_s = 10/3(N+5) \text{ tons/ft}^2$	Sand Clayey Sand	Screw Plate Tests	Below water table
Farrent (1963)	$E_s = 7.5(1-m^2)N \text{ tons/ft}^2$ $m = \text{Poisson's ratio}$	Sand	Terzaghi and Peck loading settlement curves	
Begemann (1974)	$E_s = 40 + C(N-6)$ for $N > 15 \text{ kg/cm}^2$ $E_s = C(N+6)$ for $N < 15 \text{ kg/cm}^2$ $C = 3(\text{silt with sand})$ to $12(\text{gravel with sand})$	Silt with sand to gravel with sand		Used in Greece
Trofimenkov (1974)	$E_s = (350 \text{ to } 500) \log N$ ( $\text{kg/cm}^2$ )	Sand		USSR practice

Notes:

N is penetration resistance in blows per 30 cm. (blows/ft.)

$E_s$  = soil modulus

$e$  = void ratio

**Figure 16 Elastic Modulus for SPT Data**

**Table 4.4 Other Expressions for Soil Modulus from SPT**

Equation	Soil Type	Reference
$E_s^{4/3} = (44N) \text{ (tsf)}$	Sand	Chaplin (1963)
$E_s = 48 + 4N \text{ (tsf)}$	Sand	Webb (1969)
$E_s = 7(N)^{0.5} \text{ (MPa)}$	Sand	Denver (1982)
$E_s = 3.5N \text{ to } 40N \text{ (MPa)}$	Sand	Clayton et al. (1980)
$E_s = 7.5 + 0.8N \text{ (MPa)}$	Sand	Papadopoulos (1982)

**Figure 17 Elastic Modulus for SPT (continued)**

## 2.6 Cone Penetration Test

The modulus of soils has also been correlated to the results of tip resistance measurements ( $q_c$ ) obtained from the CPT test. Most early correlations between  $q_c$  and  $E$  were of the general form:

$$E = \alpha * q_c$$

Where:

$\alpha$  = (empirical factor)

Since the performance of the CPT involves considerably less variation than the SPT and is prone to less errors in execution, it is suspected that the primary source of scatter indicated in Tables 4.5 and 4.6, and for that matter in Tables 4.3 and 4.4 is the soil itself and not the test method. Variations in soil mineral composition, initial void ratio, grain-size distribution, stress history, etc., as well as differences in initial effective stress level (octahedral) and change in stress during loading result in differences in the "operational" or "apparent" modulus of elasticity producing deformation. These factors, combined with the stress and strain level dependency of a "local" soil modulus for a given application all affect the reported correlations between the so-called soil modulus and in situ test results.

In recent years, the use of large calibration chamber tests on reconstituted samples of sands have helped to elucidate certain key variables that can influence correlations between modulus and CPT results. For both normally consolidated and over-consolidated sands, the ratio of constrained modulus,  $M$ , to CPT tip resistance,  $q$  decreases with increasing relative density, all other factors being equal. Kulhawy and Mayne (1990) have summarized a number of available chamber test results which are shown in Figure 4.20.

Jamiolkowski et al. (1988) have also noted that for a given sand the ratio  $M/q$ , and  $E/q$ , is clearly related to stress history and current stress level for sands at different relative density.

Because of the wide range in correlation constants that may exist between the results of in situ penetration tests and a singular value of soil modulus it is doubtful that any method which relies on these techniques for the accuracy of settlement estimates will be of much value, other than that created by local correlations developed from full scale field observations of performance. However, there are several techniques that have recently been suggested that account for nonlinearity in modulus and show distinctly strong correlations between observed "operational" modulus and the results of SPT or CPT tests. These methods are discussed further in subsequent sections of this report.

**Table 4.2 Estimates of Soil Modulus from SPT and CPT (after Bowles 1988).**

Soil	SPT	CPT
Sand (normally consolidated)	$E_s = 500(N + 15)$ $E_s = (15000 \text{ to } 22000) \ln N$ $E_s^{\S} = (3500 \text{ to } 50000) \log N$	$E_s = 2 \text{ to } 4q_c$ $E_s^{\dagger} = (1 + D_r^2)q_c$
Sand (saturated)	$E_s = 250(N + 15)$	
Sand (overconsolidated)	$E_s^{\ddagger} = 18000 + 750N$ $E_{s(\text{OCR})} = E_{s(\text{nc})} (\text{OCR})^{1/2}$	$E_s = 6 \text{ to } 30q_c$
Gravelly sand and gravel	$E_s = 1200(N + 6)$ $E_s = 600(N + 6) \quad N \leq 15$ $E_s = 600(N + 6) + 2000 \quad N > 15$	
Clayey sand	$E_s = 320(N + 15)$	$E_s = 3 \text{ to } 6q_c$
Silty sand	$E_s = 300(N + 6)$	$E_s = 1 \text{ to } 2q_c$
Soft clay	-----	$E_s = 3 \text{ to } 8q_c$

Notes:

$E_s$  in kPa for SPT and units of  $q_c$  for CPT; divide kPa by 50 to obtain ksf.

N values should be estimated as  $N_{60}$  and not  $N_{70}$

$\dagger$  Vesic' (1970)

$\ddagger$  Author's equation from plot of D'Appolonia et al. (1970).

$\S$  USSR (and may not be standard blowcount N).

**Figure 18 Modulus from SPT and CPT (after Bowles 1988)**



**Table 4.5 Soil Modulus from Cone Penetration Test  
(modified from Mitchell and Gardner 1975)**

Reference	Relationship	Soil Types	Remarks
Buisman (1940)	$E_s = 1.5q_c$	Sands	Over predicts settlements by a factor of about two
Trofimenkov (1964)	$E_s = 2.5 q_c$ $E_s = 100 + 5 q_c$	Sand	Lower limit Average
De Beer (1967)	$E_s = 1.5 q_c$	Sand	Overpredicts settlements by a factor of two
Schultze and Melzer (1965)	$E_s = (1/m_v)v\sigma^{0.572}$ where $v = 301.1 \log q_c - 382.3p_c$ $+ 60.3 \pm 50.3$	Dry Sand	Based of field and lab penetration tests compressibility based on $e$ , $e_{max}$ and $e_{min}$ Correlation coefficient = 0.778 for 90 tests valid for $p_c = 0$ to 0.8 kg/cm <sup>2</sup>
Bacheher and Perez (1965)	$E_s = \alpha q_c$		
	$\alpha = 0.8-0.9$	Sand	
	$\alpha = 1.3-1.9$	Silty sand	
	$\alpha = 3.8-5.7$	Clayey-sand	
	$\alpha = 7.7$	Soft clay	
De Beer (1967)	$A = C(A_{ood}/C_{ood})$	Over-consolidated sand	C from field tests $A_{ood}$ and $C_{ood}$ from lab oedometer tests $C_{ood} = 2.3(1+e)/C_c$ $A_{ood} = 2.3(1+e)/C_s$
Thomas (1968)	$E_s = \alpha q_c$ $\alpha = 3 - 12$	3 sands	Based on penetration and compression tests in large chambers Lower values of $\alpha$ at higher values of $q_c$ ; attributed to grain crushing

**Figure 19 Soil Modulus from CPT (from Mitchell and Gardner)**

**Table 4.5 Cont'd**

Reference	Relationship	Soil Types	Remarks
Webb (1969)	$E_s = 2.5(q_c+30)$ , tsf	Sand below water table	Based on screw plate tests Correlated well with settlement of oil tanks
	$E_s = 1.67(q_c+15)$ , tsf	Clayey sand below water table	
Meigh and Corbett (1969)	$E_s = 1/m_v = \alpha q_c$	Soft silty clay	
Vesic (1970)	$E_s = 2(1+D_r^2)q_c$ $D_r =$ relative density	Sand	Based on pile load tests and assumptions concerning state of stress
Schnertmann (1970)	$E_s = 2q_c$	Sand	Based on screw plate tests $\Delta\sigma = 2$ tsf

Table 4.5 Cont'd

Reference	Relationship	Soil Types	Remarks
Bogdanovic (1973)	$E_s = \alpha q_u$		Based on analysis of silo settlements over a period of 10 years
	$q_u > 40 \text{ kg/cm}^2$ $\alpha = 1.5$	Sands, sandy gravels	
	$20 < q_u < 40$ $\alpha = 1.5 - 1.8$	Silty saturated sands	
	$10 < q_u < 20$ $\alpha = 1.8 - 2.5$ $5 < q_u < 10$ $\alpha = 2.5 - 3.0$	Clayey silts with silty sand and silty saturated sands with silt	
Schmertmann et al. (1978)	$E_s = 2.5 q_u$	NC sands	$L/B = 1$ to 2 axisymmetric
	$E_s = 3.5 q_u$	NC sands	$L/B \geq 10$ plane strain
DeBeer (1974b)	$C > 3/2(q_u/\sigma_v)$	NC sands	Belgian practice
	$A > \varepsilon 3/2(q_u/\sigma_v)$	OC sands	$3 < \varepsilon < 10$ , Belgian practice
	$E_s = 1.6 q_u - 8$	Sand	Bulgarian practice
	$E_s = 1.5 q_u$ , $q_u > 30 \text{ kg/cm}^2$ $E_s = 3 q_u$ , $q_u < 30 \text{ kg/cm}^2$	Sand	Greek practice
	$E_s > 3/2 q_u$ or $E_s = 2 q_u$	Sand	Italian practice
	$E_s = 1.9 q_u$ $E_s = 2.5(q_u + 3200)$ , kPa $E_s = 1.67(q_u + 1600)$ , kPa	Sand Fine to Medium sand Clayey sands, $PI < 15\%$	South African practice
	$E_s = \alpha q_u$ , $1.5 < \alpha < 2$	Sands	U.K. practice
Trofimov (1974)	$E_s = 3 q_u$	Sands	U.S.S.R. practice
	$E_s = 7 q_u$	Clays	
Alperstein and Leifer (1975)	$E_s = (11 - 22)q_u$	Overconsolidated sand	$E_s$ determined by lab tests on reconstituted samples of sand
Dahlberg (1974)	$E_s = \alpha q_u$ $1 < \alpha < 4$	NC and OC sand	$E_s$ back-calculated from screw plate settlement using Buisman-DeBeer and Schmertmann methods; $\alpha$ increases with increasing $q_u$

Figure 20 Different Correlations for Calculating Modulus (various)

**Table 4.6 Other Expressions for Soil Modulus from CPT**

Expression	Soil	Reference
$E_s = 11q_c$	Sand	Lambrechts and Leonards (1978)
$E_s = 2.5q_c$	Sand	Roth et al. (1982)
$E_s = \alpha q_c$ $\alpha = 1.7$ to $4.4$ average = $2.5$	Med. sand	Das Neves (1982)
$E_s = 8(q_c)^{0.5}$ , $q_c$ in MPa	Sand	Denver (1982)
$E_s = 2.9q_c$	Sand	Garga and Quin (1974)

**Figure 21 Different Correlations for Calculating Modulus (continued)**

# METHODOLOGY

## 3.1 Design Chart Methodology

### 3.1.1 Input Data

In input data you have to define the parameters

Non- cohesive soils:

- Shape
- Poisson's Ratio
- L/B ratio in the form of Length and Breadth
- Footing Depth "D"
- Depth of Water Table  $D_w$
- Relative Density  $D_r$
- Unit weight  $\gamma$
- SPT N value
- CPT  $q_c$  value
- OCR/NC
- Soil type

The option to identify multiple layers has been included to accommodate changes in Soil Parameters (layer of Silty Sand over Medium Gravel for example). The depth to incompressible strata will be taken as the depth to the bottom of last layer identified in the layer Input Window. In the case of the thickness of the first layer exceeding the width of foundation, it is recommended to divide the first layer into 2 or 3 sublayers to ensure correct computations.

### **3.1.2 Bearing Capacity Calculations**

Some data given in input were utilized to get bearing capacity for that particular soil. Two methods were used.

- Meyerhof
- Teng

Terzaghi used limit equilibrium method to compute bearing capacity. It was the first limit equilibrium method which was accepted by worldwide. Later on Meyerhof (1963), Brinch Hansen (1970) and then Vesic's formulation appeared in 1973 that is based on experimental results redefined the method.

### **3.1.3 Settlement Calculations**

#### **3.1.3.1 Non-Cohesive Soil**

Schmertmann's method is preferred over other methods that are purely empirical, because it is based on physical model of settlement which has been calibrated using empirical data. Sivakugan and Johnson (2004) made a comparison between different methods: Schmertmann et al. give relatively more accuracy as compared to that of "Burland and Burbidge" (empirical method). With improvement in defining Influence factors, accuracy of Schmertmann's method is improved.

#### **3.1.3.2 Using Automated Workbook**

Automated Microsoft excel sheets were made for ease of use

- Input required data
- Click "Compute Settlement" to compute
- Click "compute Settlement Controlled Q" to compute back calculated Bearing capacity for 1 inch of settlement

### 3.1.3.3 Correlations

We have friction angles of general soils, from that we can calculate SPT N blowcount using correlation. Other correlation used was to inter-convert SPT N blowcount data and CPT ( $q_c$ ) data that inputs the mean grain size of soil  $D_{50}$ .

The correlation used are:

- SPT N Value – Friction Angle of Soil by CARTER & BENTLEY 1991
- Kulhawy & Mayne Correlation for Mean Grain Size and CPT/SPT

### 3.1.3.4 Calculation of Elastic Modulus

As determining the soil elastic modulus is the most important factor in calculating the settlement. In the case of absence of soil test data the following procedure could be done.

First determining the friction angle  $\phi$  of the soil, after which the SPT (N value) could be obtained by using correlation between friction angle  $\phi$  and SPT blow count (N) shown in figure 15

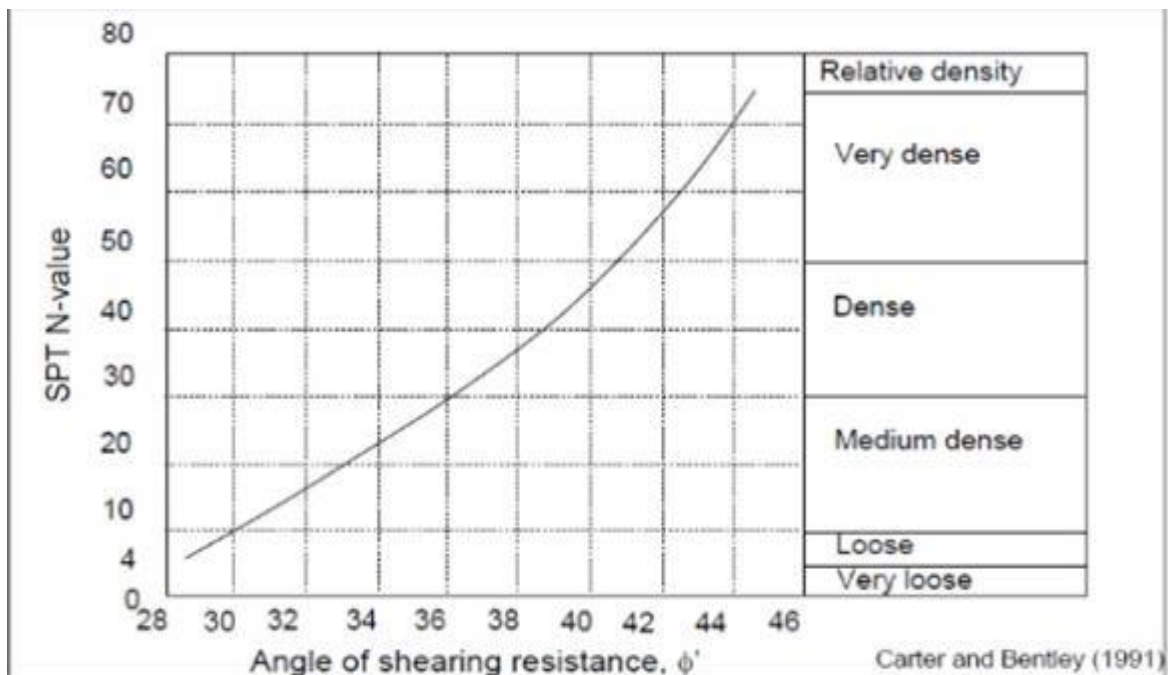


Figure 22 Correlation of N and phi  $\phi$

Now by using the correlation “Kulhawy & Mayne Correlation” for Mean Grain

Size and CPT, SPT Kulhawy & Mayne correlation,

$$q_c/N = \text{func}(D_{50})$$

$$q_c = N * \text{func}(D_{50})$$

by using this equation  $q_c$  is obtained in terms of  $D_{50}$  which is then can be used in the settlement sheets for obtaining  $E$  in terms of  $D_{50}$  and then  $E$  can be easily calculated.

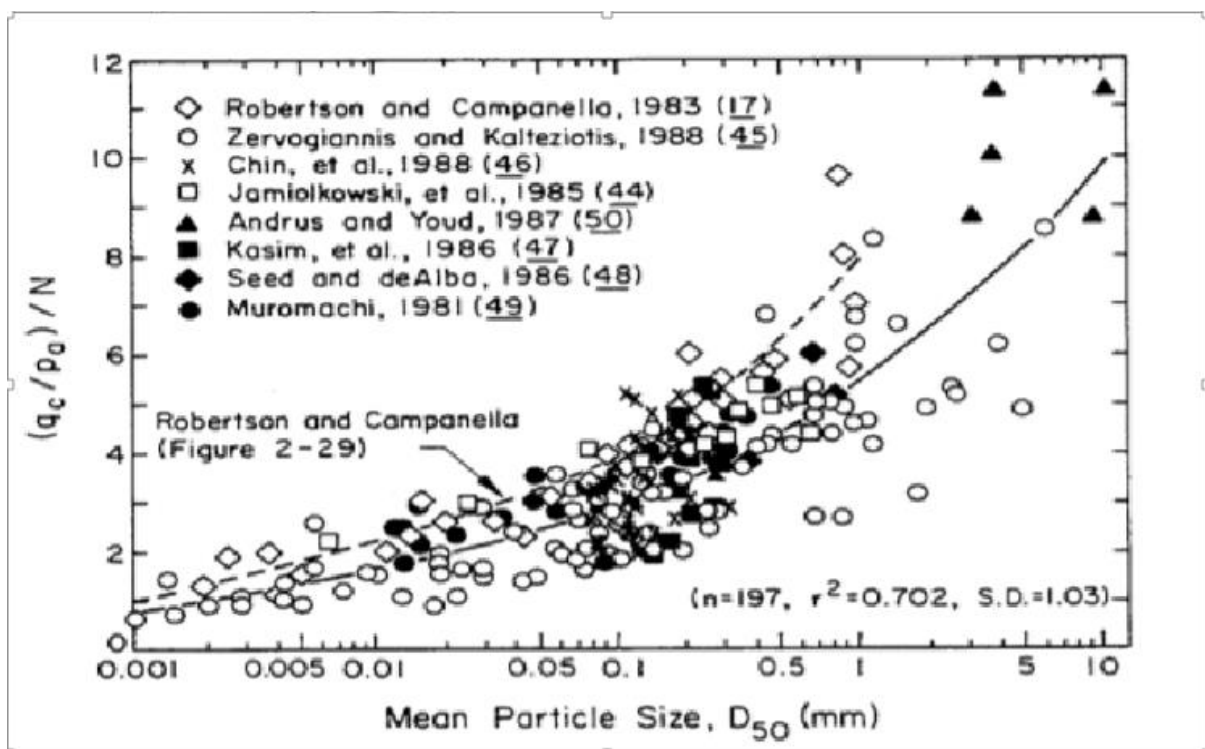


Figure 23 Kulhawy & Mayne (1991) Correlation

### 3.1.3.5 Friction Angles of General Granular Soils

Coarse Gravel	40
Medium Gravel	36
Fine Gravel	30
Coarse Sand	36-38

Medium Sand	32
Fine Sand	28

**Swiss Standard SN 670 010b, Characteristic Coefficients of soils, Association of Swiss Road and Traffic Engineers.**

### **3.1.4 Correlation of Elastic Modulus and Mean Grain Size**

1. The first pre requisite for calculation of elastic modulus from the mean grain size was availability of ranges of mean grain sizes for different kind of granular soils.
2. The ranges of different mean grain sizes were given in Kulhawy & Mayne (1991).
3. For each soil type, the typical value of angle of friction were obtained from the data above.
4. The graph between SPT blowcount and angle of friction in Carter and Bentley (1991) was digitized and it the subsequent equation was used the angle of friction from (3) to obtain designated values of blowcounts.
5. The digitized graph of Kulhawy & Mayne yielded an equation of  $\frac{q_c}{N}=5.44*D_{50}^{0.2778}$
6. Inputting values of SPT blowcount from (4) into (5), the values of  $q_c$  were obtained in terms of mean grain size.
7. Inputting the results from (6) into our spreadsheets correlations for computing modulus of elasticity we obtained ranges of modulus of elasticity including the maximum, the minimum and the average modulus in terms of mean grain size.
8. The values of mean grain size from (1) were input into the results from (7) to obtain values of modulus of elasticity.
9. The final step including plotting the modulus of elasticity ranges obtained in (8) on a graph with the variable  $W = D_{50}^{0.2778}$  (for ease of computations) on the X axis.
10. The line of best was plotted and the equation was calculated using MS EXCEL's Line of best fit tool.



### **3.1.5 The Term W**

For ease of usage and computations, this project identifies a new variable referred to as “W” and takes it to be equal to  $D_{50}^{0.2778}$ . The reason was to create ease for calculation of a line of best fit, since the Kulhawy and Mayne’s correlation provides an expression for  $q_c/N$  in terms of  $D_{50}^{0.2778}$ . The whole of the subsequent calculation steps involves expressions in terms of  $D_{50}^{0.2778}$ . Hence, identifying a new variable makes it easier for the procedure to proceed.

### **3.2 Additional Feature**

Sometimes the soil test data is not available on such cases correlations have been developed to estimate the soil test data and to achieve the required results. The correlations used consists of two main things which have to be used for calculations

- Gradation Curve

#### **3.2.1 Gradation Curve**

Gradation curve is used when the soil tests data is not available for some reason. Gradation curve give the mean grain size from which the elastic modulus of soil could be calculated by using different relations.

### **3.3 Soil test data**

The soil test data comprises of soil penetration test (no of blow counts) and cone penetration test ( $q_c$  value) has to be known for calculating or determining the settlement. But if the tests are not yet performed or the test are out of the budget the correlations could be used for estimation of N (no. of blow counts per foot) and cone penetration test value ( $q_c$ ).

## **3.4 Output of Spreadsheet**

The output of the project is in the following forms

- Elastic modulus
- Settlement
- Elastic Modulus of Soil from Mean Grain Size  $D_{50}$

### **3.4.1 Settlement**

In case of soil settlement by using different methods for calculating the outputs are

- Maximum settlement
- Minimum settlement
- Average settlement

The major output of this project is comparison of different methods in terms of maximum settlement, minimum settlement and average settlement which gives better understanding of settlement and shows which method gives more reasonable result.

### **3.4.2 Elastic Modulus**

The elastic modulus of soil is calculated by using different correlations are as follows

- Maximum elastic modulus
- Minimum elastic modulus
- Average elastic modulus

RESULTS AND DISCUSSIONS

4.1 Design Charts

The correlation between E and D<sub>50</sub> for different kinds of soil types is given below

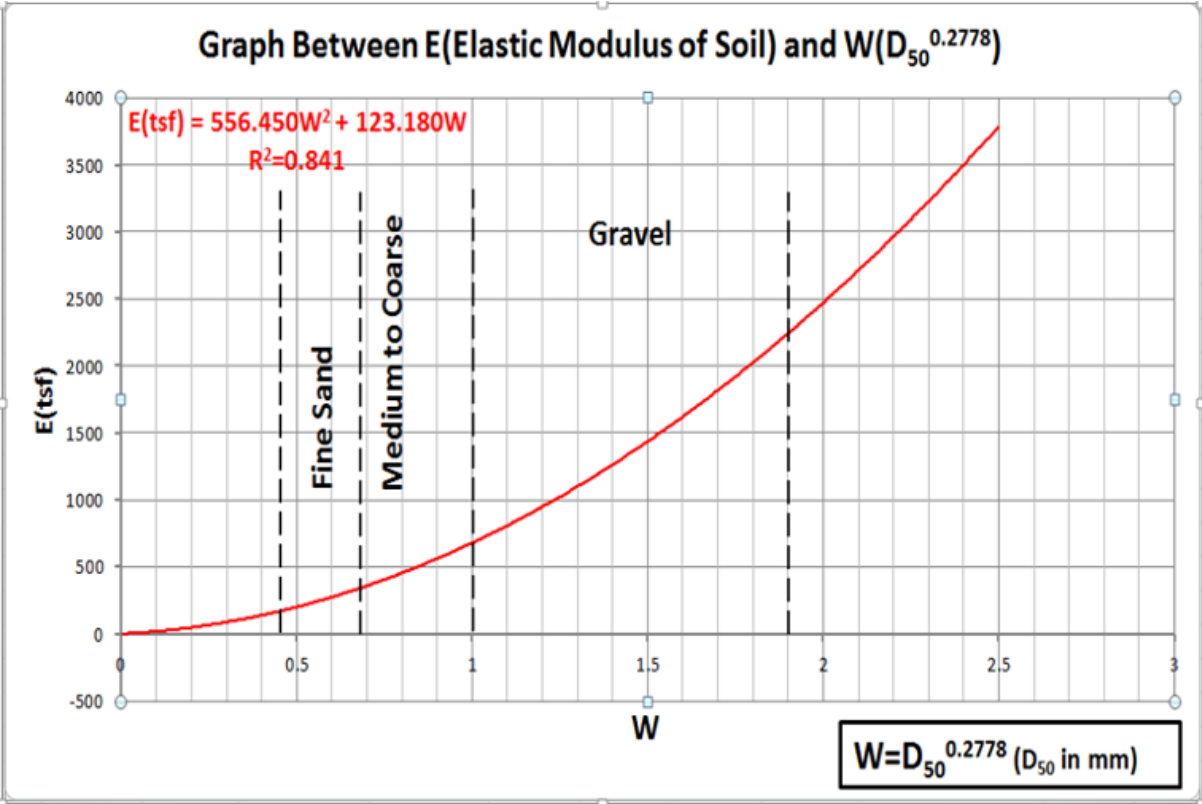


Figure 24 Proposed Relation between W and Elastic Modulus in tsf

## 4.2 Settlement Spread Sheets

### 4.2.1 Home Page

The home page of the spread sheets we make shows the

- Inputs that are given by the user
- Footing parameters
- Loading data
- Settlement calculation data
- Soil modulus data
- Layer data (field testing).

User Inserted Inputs		COMBINED WORKSHEET FOR SETTLEMENT COMPUTATIONS WITH VARIED MODULUS OF ELASTICITY				Soil Modulus Calculation Data			
Unit Input		Settlement Calculation Data				Soil Modulus Calculation Data			
Unit System	Imperial	Maximum	Minimum	Calculation Closest to Average	Comparison Box	Layer	Maximum E (ksi)	Minimum E (ksi)	Average for each layer (ksi)
Footing Parameters		Method				Method			
Length	4 ft	Tschubaroff				Lambrecht & Leonards (1973)			
Width	4 ft	Chapin & Carter				Chapin (1963)			
Embedment	2 ft	Schmertman 1996				Schmertman (1978)			
Footing Type	Square	Eused							
Formula for q	Teng								
Loading Data									
Sub surface Data									
Test Type	SPT								
Soil Data									
OC or NC?	NC								
water table at	20 ft								
Poisson Ratio	0.3								
Data Type									
no granular Curve	No								
Settlement Controlled Q									
Value Type	Value (ksi)								
Q maximum	32.71240658								
Q minimum	1.152440661								
Q average	9.880201357								
Layer Data (Field Testing)									
Layer	thickness (ft)	Gamma UnSat	Gamma Sat (lb/ft <sup>3</sup> )	Field Blow Count (N)	Soil Type	Clean or Dirty	D <sub>50</sub> (mm)		
1	2	100	105	30	Medium Sands	clean	assume		
2	2	100	105	35	Course Sands	clean	assume		
3	2	100	105	18	Fine Sands	clean	assume		

Figure 25 General Overview of Home page of Settlement Sheet

### 4.2.1.1 Input Section

Input section comprises of

- unit input section
- footing parameters
- loading data
- sub- surface data
- soil data, data type.

User Inserted Inputs		
<b>Unit Input</b>		
Unit System	Imperial	
<b>Footing Parameters</b>		
Length	4	ft
Width	4	ft
Embedment	2	ft
Footing Type	Square	
Formula for q	Teng	lbf/ft2
<b>Loading Data</b>		
Loading Type	"Simple"	
<b>Sub surface Data</b>		
Test Type	SPT	
Test Correlation	Robertson	
<b>Soil Data</b>		
OC or NC?	NC	
water table at:	20	ft
Poisson Ratio (v)	0.3	-
<b>Data Type</b>		
Is gradation Curve available ?	No	

Figure 26 Data Input Section - Foundation Inputs

Layer Data (Field Testing)							
Layer	thickness (ft)	Gamma UnSat. (lbf/ft3)	Gamma Sat. (lbf/ft3)	Field BlowCount (N)	Soil Type	Clean or Dirty	D <sub>50</sub> (mm)
1	2	100	105	30	Medium Sands	clean	assume
2	2	100	105	35	Coarse Sands	clean	assume
3	2	100	105	19	Fine Sands	clean	assume
4	2	100	105	21	Medium Sands	clean	assume
5	2	100	105	25	Medium Sands	clean	assume
6							
7							

Figure 27 Data Input Section - Soil Layer Inputs

#### **4.2.1.1.1 Unit Type**

The unit types selected for the spread sheets are

- Imperial Units.
- SI Units

#### **4.2.1.1.2 Footing Parameters**

The footing parameters consist of

- Length
- Width
- Embedment
- footing type
- formula for q

#### **4.2.1.1.3 Testing Data**

The data of the soil for which the soil test data has to calculate by using correlations has to be put in this section.

#### **4.2.1.1.4 Soil Data**

The soil data comprises of the following

- OC or NC
- Water table depth
- Poisson's ratio

#### 4.2.1.1.5 Gradation Curve Data

The gradation curve helps us to estimate the mean grain size which further gives the friction angle of the soil.

#### 4.2.1.2 Output Section

Output section comprises of

- Maximum settlement
- Minimum Settlement
- Average Settlement
- Comparison of Settlement
- Elastic Modulus Computations (max, min)

<b>COMBINED WORKSHEET FOR SETTLEMENT COMPUTATIONS WITH VARIED MODULUS OF ELASTICITY</b>				
<b>Settlement Calculation Data</b>				
	<i>Maximum</i>	<i>Minimum</i>	<i>Settlement Calculation Closest to Average of all stages</i>	<b>Comparison Box</b>
<i>Method</i>	<i>Tschebatarioff</i>	<i>Christian &amp; Carrier</i>	<i>Schmertsman 1996</i>	<b>CFM</b>
<i>E used</i>	<i>Chaplin (1963)</i>	<i>Lambrechts &amp; Leonards (1978)</i>	<i>Chaplin (1963)</i>	<b>Schmertsman (1978)</b>
Layer 1	0.372600349	0.201292292	0.371693836	0.044139909
Layer 2	0.759629607	0	0.41389033	0.02510623
Layer 3	1.991241038	0	0.392665154	1.455986974
Layer 4	1.847245273	0	0.121423246	0.070981992
Layer 5	1.620817169	0	0	0.0733676
Layer 6	0	0	0	0
Layer 7	0	0	0	0
<b>Settlement (sum)</b>	<b>6.5915 in</b>	<b>0.2013 in</b>	<b>1.2997 in</b>	<b>1.6696 in</b>

Figure 28 Output Section - Settlement Maximum, Minimum and Comparison Box

<b>Soil Modulus Calculation Data</b>			
<i>Layer</i>	<i>Maximum E (tsf)</i>	<i>Minimum E (tsf)</i>	<i>Average for each layer (tsf)</i>
<i>Method</i>	<i>Lambrechts &amp; Leonards (1978)</i>	<i>Chaplin (1963)</i>	
Layer 1	435.9229693	130.2140814	216.6898789
Layer 2	524.2084227	150.2654103	245.4791784
Layer 3	531.6436746	191.0049023	267.8544275
Layer 4	871.8459386	218.9931086	398.8283467
Layer 5	1017.153595	245.8332035	458.5991897
Layer 6	0	0	0
Layer 7	0	0	0
<b>Wiegthed Average</b>	<b>676.155</b>	<b>180.602</b>	<b>317.490</b>

Figure 29 Output Section - Modulus of Elasticity

VERIFICATION OF RESULTS

5.1 Verification using Settle 3D

Multiple Examples were solved

- Results compared with average settlement from our sheet.
- Values of Modulus calculated using our chart was compared with the values suggested in SETTLE 3d

5.1.1 Example1: SETTLE – 3D (Settlement)

We solved the following problem on settle-3D

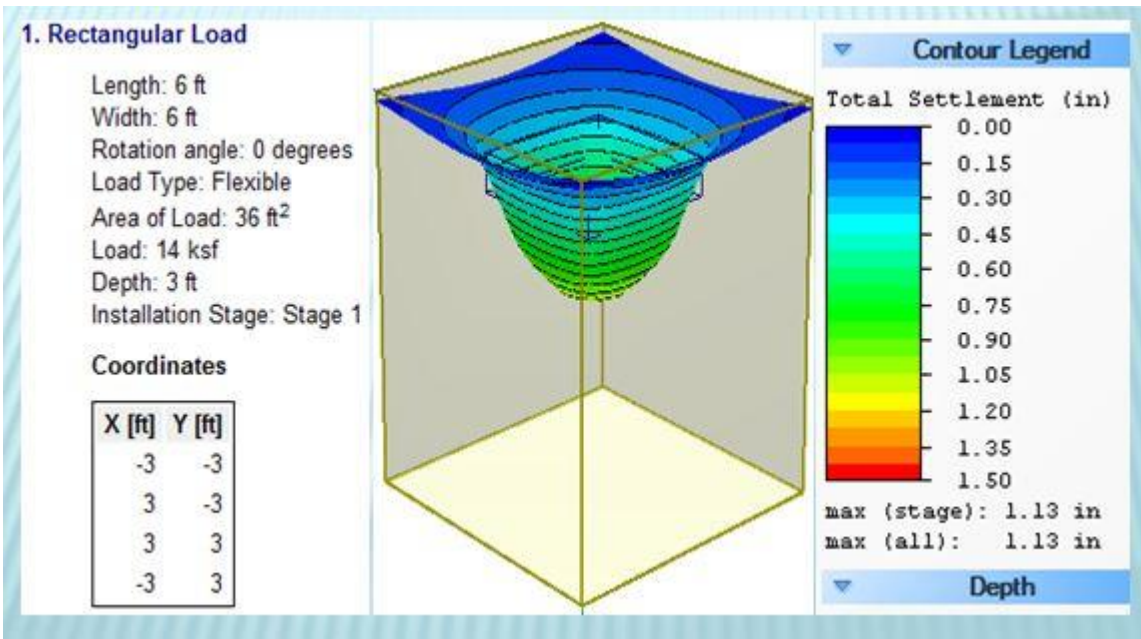


Figure 30 SETTLE 3d Example Input Data & Settlement Calculated



## 5.1.2 Example 1: Spread Sheet (Settlement)

The same data was input into our spreadsheet

User Inserted Inputs			COMBINED WORKSHEET FOR SETTLEMENT COMPUTATIONS WITH VARIED MODULUS			
Unit Input			Settlement Calculation Data			
Unit System	Imperial		Maximum	Minimum	Settlement Calculation Closest to Average of all stages	
Footing Parameters			Method	Tschebatarioff	Christian & Carrier	Schmertsman 1970
Length	6	ft	E used	Chaplin (1963)	Lambrechts & Leonards (1978)	Bogdanovi
Width	6	ft	Layer 1	0.297939582	0.234398083	0.117055543
Embedment	3	ft	Layer 2	0.638694985	0	0.21693234
Footing Type	Square		Layer 3	1.474600784	0	0.58935134
Formula for q	(User Input) Q	lb/ft <sup>2</sup>	Layer 4	2.085862337	0	0.376249961
Loading Data			Layer 5	1.830185487	0	0.105349989
Footing pressure	7	tsf	Layer 6	0	0	0
Sub surface Data			Layer 7	0	0	0
Test Type	SPT		<b>Settlement (sum)</b>	<b>6.3273 in</b>	<b>0.2344 in</b>	<b>1.4049 in</b>
Test Corelation	Robertson					
Soil Data						
OC or NC?	NC					
water table at:	10	ft				
Poison Ratio (v)	0.3	-				

Figure 31 Calculated Settlement on Spreadsheet for the example data

## 5.1.3 Results of Example 1 (Settlement)

Settlement from Settle 3D:

- Settlement = 1.13 in

Settlement from our sheet:

- Settlement = 1.40 in

So, answers generated by our automated workbook are close to the answers yielded by Settle-3D.

## 5.2 Examples: Elastic modulus and mean grain size relation

Verified from:

- General ranges of Elastic modulus values known

- Calculating Settlement from our relation of E and  $D_{50}$  and comparing with average settlement on other Es (Elastic Modulus)

## 5.2.1 Verification of E & $D_{50}$ relation

### 5.2.1.1 Example 1

Spreadsheet:

$$D_{50} = 0.5\text{mm}$$

$$E = 480\text{ tsf}$$

$$\text{Settlement} = 0.84\text{ in}$$

Settle 3D:

$$E = 480\text{ tsf}$$

$$\text{Settlement} = 0.86\text{ in}$$

### 5.2.1.2 Example 2

Spreadsheet:

$$D_{50} = 2\text{mm}$$

$$E = 970\text{ tsf}$$

$$\text{Settlement} = 0.7\text{ in}$$

Settle 3D:

$$E = 970\text{ tsf}$$

$$\text{Settlement} = 0.45\text{ in}$$

## **LIMITATIONS AND RECOMMENDATIONS**

The following limitations were encountered in this project

- Elastoplastic Behavior of Soil.
- Non-Homogeneity of Soil.
- More settlement methods can be added.
- More Elastic Modulus relations can be added and checked.
- Our correlation can be tested from field tests or field data.
- Our correlation can be expanded to other soil types also if field data of other soil types is known that will need extensive experimentation.

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