### DESIGN AND DEVELOPMENT OF A SHIM STACK VISCOUS DAMPER

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A Final Year Project Report

Presented to

### SCHOOL OF MECHANICAL & MANUFACTURING ENGINEERING

Department of Mechanical Engineering
NUST

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In Partial Fulfillment
of the Requirements for the Degree of
Bachelor of Mechanical Engineering

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by

Muhammad Muneeb Arshad Muhammad Uzair Sajjad Azan Akhtar

June 2018

# **EXAMINATION COMMITTEE**

We hereby recommend that the final year project report prepared under our supervision by:

Muhammad Muneeb Arshad	NUST201432274
Muhammad Uzair Sajjad	NUST201433156
Azan Akhtar	NUST201432191
Titled: "Design and Development of a Shim Stack Viscous Da	amper" be accepted in partial fulfillment
of the requirements for the award of Bachelor's in Mechanica	l Engineering degree.
Supervisor: Dr. Sami ur Rahman Shah (Assistant Professor)  SMME, NUST  Committee Member: Dr. Jawad Aslam (Assistant	Dated:
Professor)	
SMME, NUST	Dated:
Committee Member: Dr. Emad Uddin (Assistant Professor)	(a)
SMME, NUST	Dated:

# **COUNTERSIGNED**

(Date)

Dated:	
	(Dean / Principal)

(Head of Department)

# **ABSTRACT**

Shock absorber is a device which is used to reduce the effect of shock impulses by damping them and dissipate kinetic energy. It is used to improve the quality of ride, as well as comfort level, by substantially reducing the magnitude of disturbances. This is specially required in locomotion of vehicles over rough or unsmooth surfaces. Spring is compressed as the vehicle encounters a bump on the road. The reaction force would cause spring to retain its normal length. Due to high momentum, spring would shoot past its normal position and this rebound would lift the body of the vehicle. The weight of vehicle is larger in comparison to this spring force. It would cause the spring to be compressed again. This process is repeated several times, with reducing magnitude. Conventional orifice dampers don't provide effective shock absorption. Shim-stack dampers have greater shock absorbing efficiency and they have already attained preferences in motor-bikes. Our project focuses on the design and development of a shim stack viscous damper. It also encompasses a comparison of its performance with a regular orifice damper.

# **PREFACE**

Motorcycles in Pakistan use a regular plunger orifice damper. The shock absorption ability of the said damper has proven to be quite low as it provides an uncomfortable ride. Other countries have already moved beyond this damper and have developed technologies like shim stack damper and spool valve damper. We have developed a shim stack damper that can absorb shocks more effectively. It is designed to increase the damping ability and efficiently reduce the shocks of a vehicle. Our device uses shim stack technology which are Belleville washers piled up on top of each other. The damping is pressure sensitive and can be adjusted by varying the pressure. A gas canister and a floating piston have also been added to prevent cavitation which occurs at frequent bumps. The main piston has a new design with holes machined at 12.81°. This innovative design helps to operate the shim stack valving technology more easily.

# **ACKNOWLEDGEMENT**

In this project, everyone we have come across was extremely helpful and encouraging. We really want to thank Dr. Sami ur Rahman Shah, our supervisor, for his exceptional cooperation and support. He has helped us at every single step of our project. Without his guidance and constructive criticism, we would never have been able to complete this project.

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We are also thankful to the staff of MRC for their help during the fabrication phase of our project.

We have gained technical and theoretical knowledge as well as learned how to tackle stressful situations in a project under the guidance of our supervision committee.

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# **NOMENCLATURE**

k Stiffness of spring

d Thickness of spring coil

D Major diameter of spring

 $\omega_n$  Natural Frequency

 $\omega_d$  Damped Frequency

 $\tau_d$  Time period of damped vibrations

 $c_c$  Critical damping constant

c Damping constant

 $\varepsilon$  Damping ratio

x Displacement of damper

 $\dot{x}$  Velocity of damper

 $F_{rebound}$  Rebound force

*P*<sub>rebound</sub> Rebound pressure

 $d_{piston}$  Diameter of piston

 $d_{rod}$  Diameter of rod

 $F_{compression}$  Compression force

 $P_{comp}$  Compression pressure

 $P_{gas}$  Gas pressure

 $t_{rebound}$  Rebound shim thickness

 $t_{compression}$  Compression shim thickness

 $D_{shim}$  Shim outer diameter

 $C_D$  Discharge coefficient

 $D_{valve}$  Major diameter of valve

 $A_{reb_{flow}}$  Area of rebound flow

 $A_{comp_{flow}}$  Area of compression flow

 $Q_{v_{reb}}$  Rebound valve flowrate

 $Q_{v_{comp}}$  Compression valve flowrate

 $Q_{lp}$  Piston leakage flowrate

l Piston circumference

b Piston height

# **CHAPTER 1: INTRODUCTION**

A very important aspect of a vehicle is a comfortable ride to the user. Comfort is related to the damping ability of the vehicle. Shock absorbers play an important role in reducing shocks and increasing the life of the vehicle. They reduce the motion of both sprung and unsprung masses of the vehicle. The sprung mass includes the components supported by the spring and unsprung mass includes the brake caliper, brake disc, wheel, tire, suspension upright and a part of the suspension arms.

The tire damps the vehicle by approximately 2% but majority of the damping is carried out by the shock absorber. Shock absorbers work like a dynamic spring i.e. they produce force proportional to their velocity.

The primary function of a shock absorber is to damp shocks at their resonant frequencies. Their secondary function is to control the rate of weight transfer during transients such as braking, corner entry and acceleration.

#### 1.1 Motivation

Keeping in mind the difficulties that a rider may face during a riding session and the life of the vehicle, we concluded that a new kind of damper is needed that can absorb shocks more effectively. So, we decided to compare the current damper used in motorcycles in Pakistan, a shim stack damper and a spool valve damper. Even though, spool valve dampers were found to be better than shim stack shock absorbers and the conventional orifice shock absorbers, we chose to proceed with the shim stack technology due to the complexities that would arise during the manufacturing of a spool valve damper. The manufactured shim stack damper would have Belleville washers as the primary component for its operation since Belleville washers are known to deflect less under high loading

conditions. These washers would restrict the oil flow through the main piston of the shock absorber to improve damping.

### 1.2 Working Principle:

Our shock absorber consists of two chambers which are connected together.

First chamber (main cylinder) contains oil, the main piston along with the shim stack and the damper rod. The main piston would move downwards during the compression stroke. The oil would be displaced upward applying a force on the shim stack at the rebound side. The main piston would go back up during the rebound stroke displacing the oil back to the bottom. Now, the oil would apply a force on the shim stack at the compression side. The oil flow would be restricted by the shim stacks on both sides which will slow down the motion of the damper rod. This would increase the efficiency of the damper.

The second chamber (gas canister) contains a floating piston with a gas on one side of the piston and oil on the other side. The introduction of a second chamber is necessary to prevent cavitation. On a bumpy road, the shock absorber would undergo frequent compression and rebound cycles which can increase the temperature of the oil. The oil may change its phase as a result and damping becomes useless. This process is called cavitation.

# 1.3 Organization of the report:

Our report is divided into four main chapters. In this chapter, an overview about our project and our motivation for doing this project is explained. The working mechanism of our damper is also explained briefly in this chapter.

In the next chapter, literature review and background information of the process is given. Moreover, the background information of the designs is also provided.

Third chapter gives detailed explanation of the process, calculations, design, analysis and our approach to solve the problems. Our calculations include force calculations, shim thickness calculations, the vibrational analysis and the fluid calculations.

Fourth chapter includes the results obtained by analysis and calculations. Fifth chapter includes the results obtained after the manufacturing and testing of our shock absorber.

# **CHAPTER 2: LITERATURE REVIEW**

A shock absorber is an inertial damper that utilizes the viscous properties of a fluid which redirects motion by forcing the fluid through a narrow passage. [1]

Shock absorbers are of different types and vary according to their construction, working and nature of the fluid used. These dampers have different applications in automotive industry depending upon the required nature of damping.

One of our deliverables was the theoretical comparison of orifice dampers, shim stack dampers and spool valve dampers which fall under the category of monotube dampers.

# 2.1 Monotube dampers: [2]

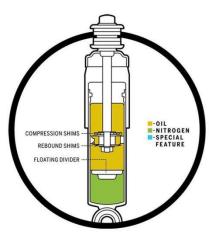


Figure 1: Monotube Damper [2]

Monotube dampers are classified on the basis of the type of the valve used in the damper. Following are the different types of valves:

- Disc Valve (Orifice damper)
- Rod Valve
- Shim Valve (Shim Stack damper)
- Spool Valve (Spool Valve damper)

#### 2.1.1 Disc Valve

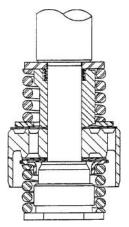


Figure 2: Disc Valve [9]

A disc valve is coupled with a spring. It is opened by attaining a feasible pressure difference. This pressure difference depends on the preload force of spring and active pressure area. This area might be greater in magnitude in comparison to the area for fluid flow. The compression of the spring depends upon its stiffness. A higher-pressure difference would cause an increase in the flow area as well as the flow rate. In practical applications, a stiff spring is not feasible; the actual flow is very minute and a large force would cause a very big flow area. This type of valve is suitable in pre-load conditions where flow constraint in one direction is required. A variation of valve can be attained using a conical spring.

#### 2.1.2 Rod Valve

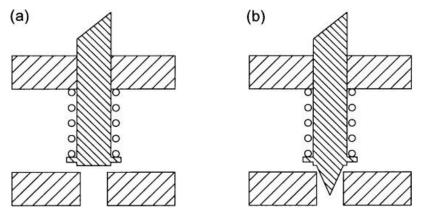


Figure 3: Rod Valve (a) Basic flat ended (b) Taper ended [9]

In rod valve, flow is kept in check by a flat rod which is present at the end of a hole. Size of the hole is dependent upon the feasibility of manufacturing. Effective limit area is limited by the equality of exit area and hole area. Spring is rather stiff, as higher uplift force is required in a small distance.

Tapered rod can be used to increase this force for the area under consideration. Long length tapered valve is known as needle valve.

# 2.1.3 Spool Valve

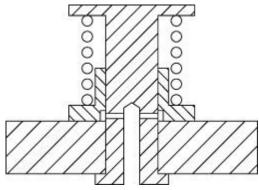


Figure 4: Spool Valve [9]

A spool valve is coupled with a coil spring. Foot valve is a spool valve with four cross-drilled holes. In order to vary flow area with spool position, the profile of exit holes is varied according to requirement. This adaptive construction is a positive aspect of spool valve. So theoretically, all required features are attainable by varying the precision of exit holes and the cost of manufacturing. Broaching is an effective technique to manufacture precise holes. In the case of a single exit spool valve, hysteresis and friction are caused due to large lateral force exertion on fluid. This can be tackled by using two symmetrically positioned exit holes. Spring stiffness ranges between 500-100 kN/m. One variation involves spool valve fixed with a base. A slider attached with it moves alongside it. The slider is controlled by a coil spring.

#### 2.1.4 Shim Valve

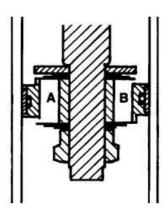


Figure 5: Shim Valve [9]

In practical use, a stack of shims with varying diameters are used instead of same diameter for variable damping. This is desirable in racing cars. These shims sit naturally on the piston without the problem of manufacturing dimensional inconsistencies affecting the preload. Shim stack on one side of the piston is controlled by three holes. Shims have varying thicknesses ranging from 0.2mm-0.5 mm. Leakage path is prevented by coning the piston surface at an angle range of 0.5°-2°. Usually, a shim stack comprises of six shims with reducing diameters allowing for adjustable stiffness. A complex shim stack arrangement requires additional support by adjusting the force before the load acts. This support is provided by an additional shim stack. Extra stiffness can be attained by spacing shim with small diameter discs. This is required for progressive increase in deflection. Radial slots

are used in shims when shim valves are dealing with large volume flow. These are supported with a rigid central support. This results in a cantilever of long length.

# 2.2 Hydraulic Fluid: [11]

A hydraulic fluid is chosen considering the following characteristics.

- Chemical Properties
- Density
- Thermal Expansion
- Compressibility
- Viscosity
- Thermal Capacity
- Thermal Conductivity
- Vapor Pressure

General choice for damper oil is basic mineral oil and its properties are given in Appendix (1).

# **2.3 Gas Additive:** [11]

The choice of the gas additive in damper depends upon the following characteristics.

- Gas density
- Gas viscosity
- Gas compressibility
- Gas absorption
- Emulsification

Nitrogen is most commonly used and its properties along with other gases are tabulated in Appendix (2).

# **CHAPTER 3: METHODOLOGY**

#### 3.1 Why Shim stack viscous damper?

Compared to the traditional disc valve damper, the shim stack damper has many advantages and the spool valve damper is better than the others in terms of precision and accuracy. However, we chose a shim stack damper since the tolerances required for the manufacturing of a spool valve damper were in microns. The equipment required for this purpose in unavailable in Pakistan. Other features of a shim stack damper are discussed below.

#### 3.1.1 Pressure Sensitive Damping

Damping is created by the fluid pressure differential inside the shock. The shims on the face of the piston resist bending, increasing fluid pressure through this.

#### 3.1.2 Adjustable damping

For oil to flow, it has to bend the shims for an opening. If the shims are thin, the oil can easily bend them, allowing a lot more oil to pass through the piston and results in little damping. If the shims are thicker, they are harder to bend and it takes more force for the oil to provide an opening through the piston, increasing the damping effect. Numerous shim stack combinations can be made in view of this fact.

#### 3.1.3 Tapered Stack Configuration

We chose a tapered stack configuration as it smoothens the bend radius at the stack clamp and helps to avoid stressing the shims beyond the yield point. The pyramidal diameter variation makes fine tuning adjustments possible. Tunable features are

- Number of shims
- Thickness of shims
- Diameter of shims

- Number and thickness of face shims
- Stack clamp diameter

### 3.1.4 Selection Criteria for the damping fluid

The hydraulic oil used should cover the following requirements.

- Reduced friction and wear between the moving parts
- Don't foam
- Prevent corrosion
- Compatibility with seal material
- Consistent damping force provision

Caltex Chevron Rando HD 68 was chosen to be used in the viscous hydraulic shock absorber because it is most readily available in the market and has properties suitable for the Pakistani environment. Its properties are given in Appendix (3).

### 3.1.5 Selection Criteria for the gas

Nitrogen is most commonly used in shock absorbers to help prevent the problem of cavitation.

Hence, it was chosen to be used in our shock absorber.

#### 3.1.6 Material Selection

We required a material for our pistons that would be compatible with the hydraulic oil and would bear the stresses when the shock absorber is operational. Conventional disc valve shock absorber has a cast iron piston. However, we chose to proceed with aluminum because

- It has lighter weight
- Loads were not that high and aluminum piston could bear them
- Its machining was cheaper

Some of its properties are:

Specification No.	6061-T6
Type/Grade	6061
Min. Tensile Strength [MPa]	310 MPa
Min. Yield Strength [MPa]	276 MPa

Table 1: Properties of Aluminum

The properties stated above were taken from Aluminum Standards and Data 2000.

This material is feasible for our project because of its low cost, high yield strength and easily available machining process in the market.

# 3.2 Concept Model:

It consists of two chambers which are connected together via a pipe. One chamber contains the viscous oil, the main piston assembly along with the shim stack. The shim stack restricts the viscous oil flow to increase damping. During the compression stroke, the oil is displaced towards the rebound side of the main piston and strikes the rebound shims with enough force to bend the shims. Similarly, during the rebound stroke, the oil is displaced towards the compression side of the main piston and strikes the compression shims with high pressure to deliver a force capable of being the shims to provide a path for the oil. During frequent cycles of vibrations, the oil tends to heat up and may change to vapor phase which might render the damping useless. The holes in the main piston are machined at an angle of 12.81° to provide a simple path for the oil to hit the shims easily without any losses. Second chamber contains the floating piston, the viscous oil and the gas. It is filled with gas under high pressure on one side of the floating piston. The high gas pressure in this chamber would provide ample resistance to the oil and prevent its phase change.

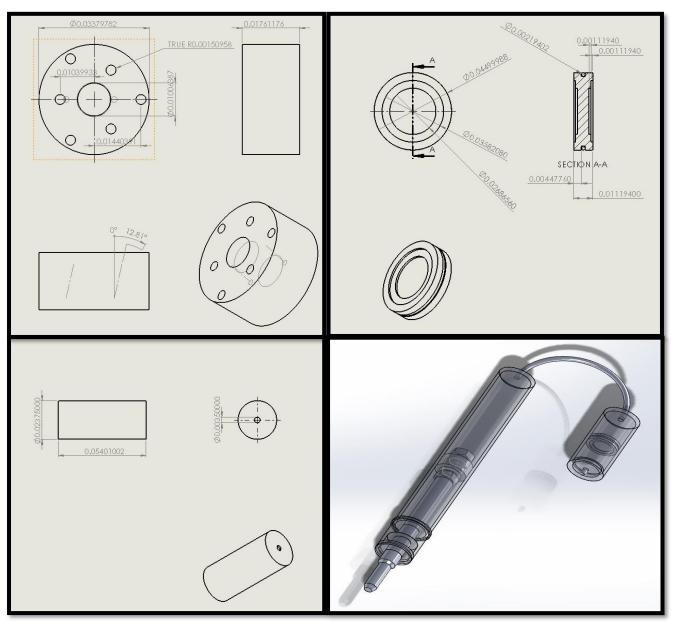


Figure 6: CAD Model of new design



Figure 7: CAD Model of old design

### 3.3 Vibrational Analysis:

The stiffness of the spring was found by reverse engineering from the following formula

$$k = \frac{d^4G}{8D^3N}$$

The spring constant was found out to be 32476.46 N/m. CG125 normally has a mass of 250kg.

$$\omega_n = \sqrt{\frac{k}{m}} = 11.4 \, rad/s$$

$$\omega_d = \sqrt{1 - \varepsilon^2} = 10.42 \, rad/s$$

Where  $\varepsilon$  was assumed to be 0.4037 since shock absorbers are usually underdamped.

$$\tau_d = \frac{2\pi}{\omega_d} = 0.603 s$$

$$c_c = 2m\omega_n = 5700 Ns/m$$

$$c = \varepsilon c_c = 2301.09 Ns/m$$

$$x = \omega_d X e^{-\varepsilon \omega_n t} = 0.1079 m$$

Generally, a frequency of 1 Hz is required for a comfortable ride. Mathematical modelling was done

 $\dot{x}_o = X\omega_d = 1.12m/s$ 

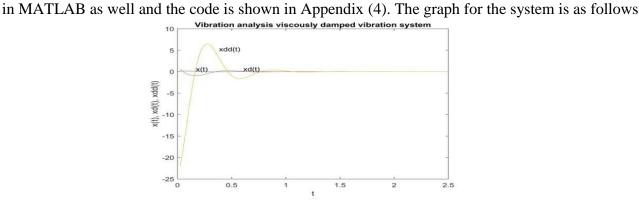


Figure 8: Displacement, velocity and acceleration w.r.t time

# 3.4 Force Calculations: [14]

When the bike is subjected to a jerk, the main piston in the hydraulic cylinder moves downward exerting a compressive force on the hydraulic oil. To move the piston back to its original position, a rebound force acts upon the piston. Generally, the hydraulic cylinders are designed so that the compressive force is about 1.6 times the rebound force.

$$F_{rebound} = \frac{P_{rebound} \times \pi (d_{piston}^2 - d_{rod}^2)}{400}$$

Where  $d_{piston} = 2.015 \ cm$ ,  $d_{rod} = 0.99 cm$ ,  $P_{rebound} = 25 bar$ 

$$F_{rehound} = 0.60478 \, kN$$

$$F_{compression} = 1.6 \times F_{rebound} = 0.96764 \ kN$$

The compression force depends on the pressure in the compression region, the pressure in the gas chamber and the area of the compression region. Hence the pressure in the gas chamber can be calculated from the following formula.

$$F_{compression} = rac{\left(P_{comp} + P_{gas}\right) imes \pi \left(d_{piston}^2 - d_{rod}^2\right)}{400}$$
 $P_{comp} = 20 \ bar$ 
 $P_{gas} = 10.34 \ bar$ 

The shims in the rebound area are subjected to the compression force and their thickness can be calculated from the following formula.

$$t_{rebound} = \frac{1}{10} \sqrt[4]{\frac{F_{compression}D_{shim}}{132.4 \ h/t}} = 0.78 \ mm$$

where the shims outer and inner diameter are 14.25mm and 6mm respectively.

Similarly,

$$t_{compression} = \frac{1}{10} \sqrt[4]{\frac{F_{rebound}D_{shim}}{132.4 \ h/t}} = 0.69 \ mm$$

The h/t ratio for the above equation were taken from the graph as shown in Appendix (5).

### 3.5 Fluid Calculations: [15]

The flowrate through the piston valves is given by the following equation

$$Q_v = A_{flow} C_D \sqrt{\frac{2(P_{compression} - P_{rebound})}{\rho}}$$

$$A_{flow} = \alpha \pi D_{valve} x$$

Talbott has used  $\alpha = 0.5$  for modelling a shock absorber in his paper for compression flow and rebound flow with three holes in the main piston. The coefficient of discharge for holes at 12.81° with vertical axis was found to be 0.51375.

$$A_{reb_{flow}} = 9.109 \times 10^{-7} \, m^2$$

$$A_{comp_{flow}} = 8.03 \times 10^{-7} \, m^2$$

$$Q_{v_{reb}} = 1.64 \, \times 10^{-5} m^3/s$$

$$Q_{v_{comp}} = 1.46 \times 10^{-5} m^3 / s$$

The viscosity of the damper oil was found to be 64.6 cSt at 40°C. The leakage flow from the piston was found by the following equation.

$$Q_{lp} = \left(\frac{\Delta P b^3}{12\mu l} + \frac{\dot{x}b}{2}\right) \pi d_{piston}$$

Where I is the circumference of the piston and b is the height of the piston.

$$Q_{lp} = (1.274 \times 10^{-5} + 5.25 \times 10^{-3} \dot{x})0.063 \ m^3/s$$

The piston leakage flowrate comes out to be a function of the damper velocity.

### 3.6 Finite Element Analysis:

The purpose for conducting a simulation test for our product is to ensure and reconfirm that the results obtained theoretically are accurate.

Since our project involves a pressure difference of about 5 bars, a simulation of the shims was done to get insight on stress that they will endure and the deformation they will undergo. Another simulation was conducted for the floating piston which must bear the compression pressure and the gas pressure. It was done to account for the stresses and deformations.

Both simulations were conducted using ANSYS R18.0.

#### 3.6.1 Material

As it was stated earlier that the material selected for the shims was spring steel and the material selected for the floating piston was aluminum.

#### 3.6.2 Pressure Simulation

Simulation was carried out considering the following pressures.

$$P_{reb} = 25 \ bar$$

$$P_{comp} = 20 \ bar$$

$$P_{gas} = 10.34 \ bar$$

### Units used for the simulation are:

Unit system	Metric (mm, kg, N, s, mV, mA) Degrees rad/s Celsius
Angle	Degrees
Rotational Velocity	Rad/s
Temperature	Celsius

Table 2: Units of simulation

# 3.6.3 *Model*

The initial model was made using SolidWorks and was later imported in ANSYS. The dimensions of the shim are given below.

Internal diameter	10.5mm
External diameter	17.4mm
Thickness	0.75mm

Table 3: Geometric model of shim

The dimensions of the floating piston are given below.

External diameter	45mm
Thickness	11mm

Table 4: Geometric model of floating piston

# 3.6.4 Contours of the analysis obtained

# Compression shim

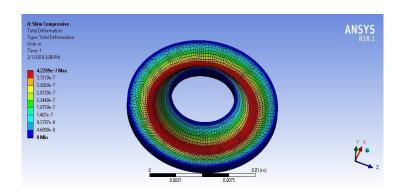


Figure 9: Total deformation (Compression Shim)

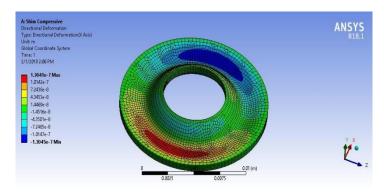


Figure 10: Directional Deformation (Compression Shim)

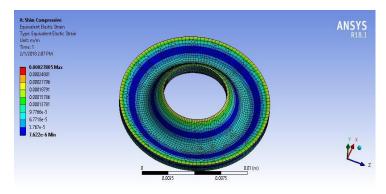


Figure 11: Equivalent Elastic Strain (Compression Shim)

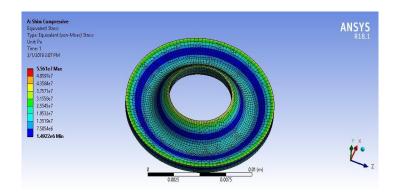


Figure 12: Equivalent Stress (Compression Shim)

## Rebound shim

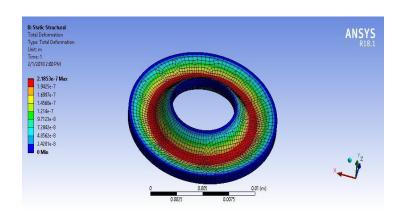


Figure 13: Total Deformation (Rebound Shim)

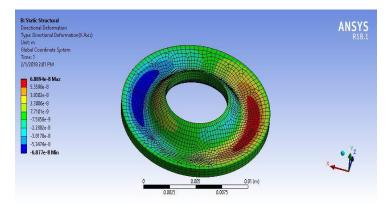


Figure 14: Directional Deformation (Rebound Shim)

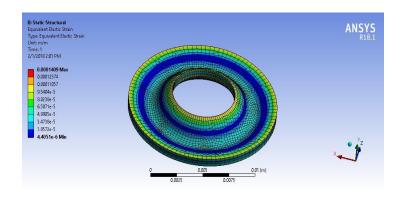


Figure 15: Equivalent Elastic Strain (Rebound Shim)

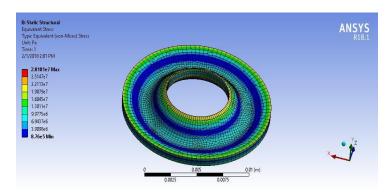


Figure 16: Equivalent Stress (Rebound Shim)

## Floating Piston

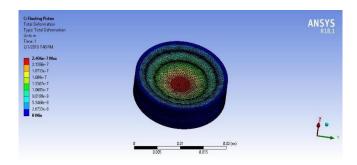


Figure 17: Total Deformation (Floating Piston)

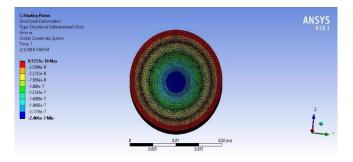


Figure 18: Directional Deformation (Floating Piston)

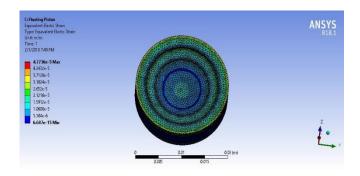


Figure 19: Equivalent Elastic Strain (Floating Piston)

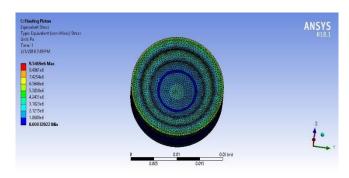


Figure 20: Equivalent Stress (Floating Piston)

## **CHAPTER 4: RESULTS AND DISCUSSIONS**

The shock absorbers were attached to the rear of a Honda CG125. The accelerometer used was from Samsung Galaxy S6. The phone was attached to the strut of the bike and the data was collected by Accelerometer Analyzer android application.

### 4.1 Disc Valve damper results:

Firstly, the original conventional disc valve damper was tested and the generated readings are in Appendix (6). The graphs obtained from these readings are as follows.

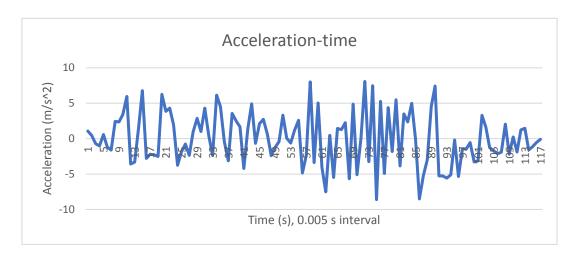


Figure 21: Acceleration time graph (Disc Valve damper)

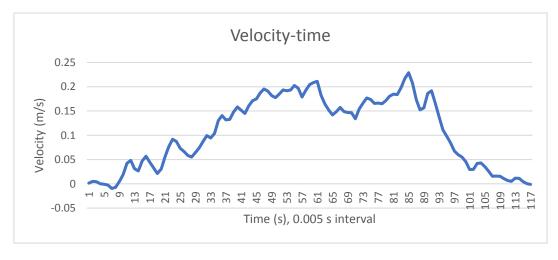


Figure 22: Velocity time graph (Disc Valve Damper)

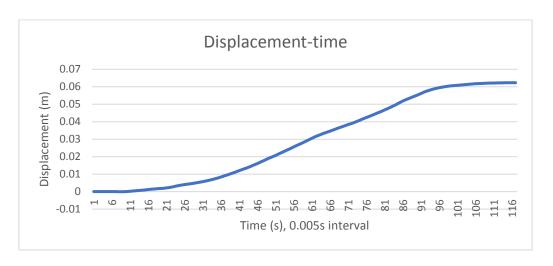


Figure 23: Displacement time graph (Disc valve damper)

## 4.2 Shim stack damper results:

Only pressure up to 2 bar was available so we took two readings, one at 1 bar and the other at 2 bar.

A place with pressure up to 5 bar available was found later. Following graphs were plotted from the two readings.

#### 4.2.1 Results at 1 bar

The generated readings are shown in Appendix (7).

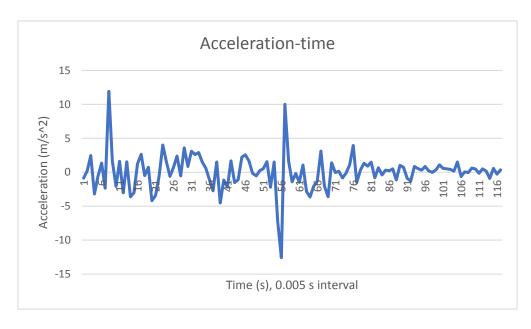


Figure 24: Acceleration time graph (Shim stack damper @ 1 bar)

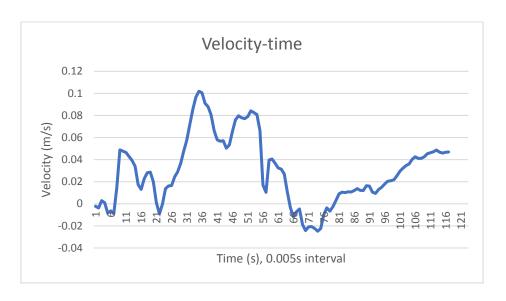
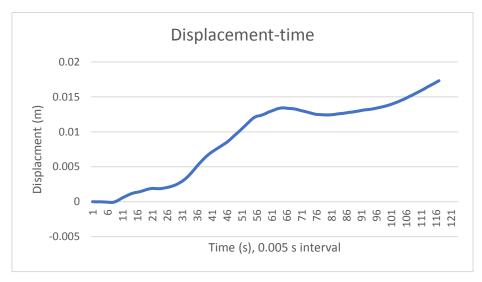


Figure 25: Velocity time graph (Shim stack damper @ 1bar)



Figure~26:~Displacement~time~graph~(Shim~stack~damper~@~1bar)

### 4.2.2 Results at 2 bar

The generated are shown in Appendix (8).

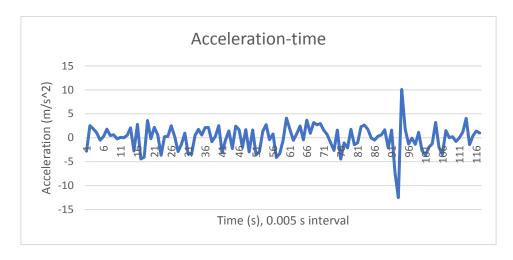


Figure 27: Acceleration time graph (Shim stack damper @ 2 bar)

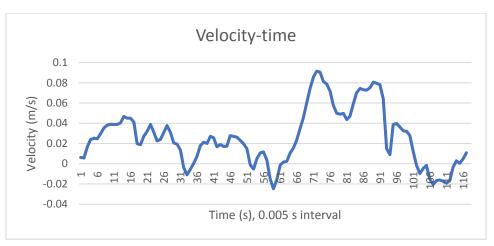


Figure 28: Velocity time graph (Shim stack damper @ 2bar)

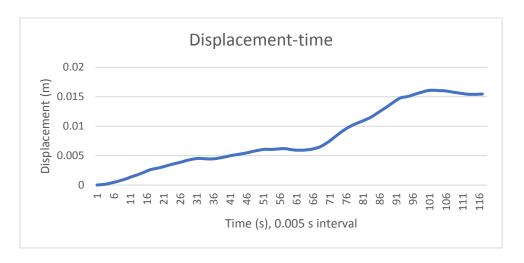


Figure 29: Displacement time graph (Shim stack damper @ 2bar)

#### 4.2.3 Results at 5 bar

The generated readings are shown in Appendix (9).

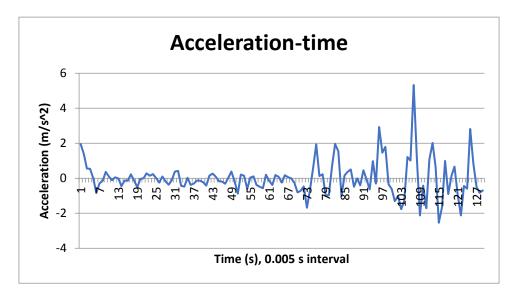


Figure 30: Acceleration time graph (Shim stack damper @ 5 bar)

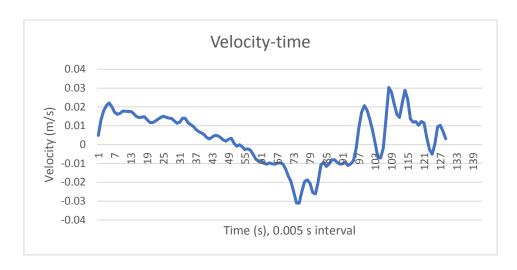


Figure 31: Velocity time graph (Shim stack damper @ 5 bar)

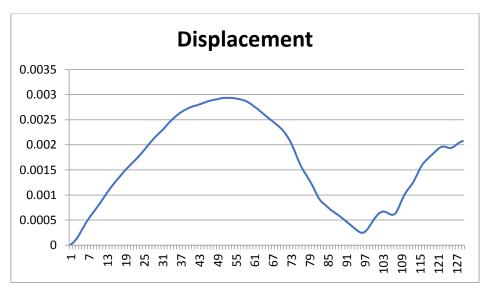


Figure 32: Displacement time graph (Shim stack damper @ 5 bar)

#### 4.3 Discussion:

In the acceleration-time graph for the disc valve damper, it is quite evident that the bike undergoes frequent jumps and the required damping is not provided. From the velocity-time graph, the damping constant for the conventional disc valve damper was found to be 2.36 Ns/mm. The maximum displacement the bike undergoes is slightly above 0.06m.

In the acceleration-time graph for the shim stack viscous damper at 1 bar pressure, the acceleration stays below  $5\text{m/s}^2$  throughout the ride except for the speed breaker where the acceleration reaches  $10\text{m/s}^2$  or slightly above it. From the velocity-time graph, the damping constant for shim stack

damper at 1 bar was found to be 2.45 Ns/mm which is about 3.8% increase in the damping constant. The maximum displacement the bike undergoes is about 0.017m which is very less compared to 0.06m.

In the acceleration-time graph for the shim stack viscous damper at 2 bar pressure, the acceleration stays below 5m/s<sup>2</sup> throughout the ride but only goes at 10m/s<sup>2</sup> at the speed breaker. From the velocity-time graph, the damping constant for shim stack damper at 1 bar was found to be 2.64 Ns/mm which is about 11.8% increase in the damping constant. The maximum displacement the bike undergoes is slightly above 0.015.

In the acceleration-time graph for the shim stack viscous damper at 5 bar pressure, the acceleration stays below 6m/s<sup>2</sup> throughout the ride. However, there are abrupt changes in the acceleration at the speed breaker. This minute error can be attributed to the vibrations the bike undergoes during gear shift. From the velocity-time graph, the damping constant for shim stack damper at 1 bar was found to be 2.72 Ns/mm which is about 15.2% increase in the damping constant. The maximum displacement the bike undergoes is slightly below 0.003.

The theoretically calculated damping value by vibrational analysis was 2.302 Ns/mm which is quite close to the values obtained from the theoretical results.

## **CHAPTER 5: CONCLUSION AND RECOMMENDATIONS**

Our project is designed on the basis of the calculations stated above. We tested our shock absorber and came to the conclusion that it works correctly as proposed i.e. the damping is pressure sensitive and it can be adjusted either by varying the pressure in the gas canister or by changing the configuration of the shim stack on the main piston.

#### **5.1 Recommendations:**

Based on the results and time limitation for fabrication, following recommendations can help improve the overall model.

- 1. The results can be improved by using a pressure up to 10 bars.
- 2. The results can be improved by using a higher quality damping fluid.
- 3. Using a less stiff spring or making the configuration of the shims less stiff to provide a less stiff and more comfortable ride.
- 4. The main cylinder can be made twin tube for better performance.
- 5. The diameter of the main cylinder and the main piston can be increased to provide more room for oil and hence, improve damping.

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common-types-work-feature

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# **Appendix I: Damper Oil Properties**

	Representative Damper oil properties (Basic mineral oil)					
1	Density @ 15°C	ρ	≈ 860	$kg/m^3$		
2	Viscosity @ 15°C	μ	≈ 40	mPa. s		
3	Temperature Range	T	$\approx -40 \text{ to} + 130$	°C		
4	Pressure Range	P	$\approx 0 \text{ to } 20$	МРа		
5	Compressibility	$(d\rho/dP)/\rho$	≈ 0.05	%/MPa		
6	Thermal Conductivity	k	≈ 0.14	W/m. $K$		
7	Thermal Capacity	$C_p$	≈ 2.5	kJ/kg.K		
8	Viscosity-temperature sensitivity	(dμ/dT)/μ	≈ -2	%/°C		
9	Viscosity-pressure sensitivity	(dμ/dP)/μ	≈ <b>+</b> 3	%/MPa		
10	Surface Tension	$\sigma_{\scriptscriptstyle S}$	≈ 25	mN/m		
11	Air absorption effect	$k_A$	≈ 1.0	kg/m³. MPa		

# **Appendix II: Physical Properties of Gases**

Physical Prop	perties of	Gases						
Gas			Argon	C <b>O</b> 2	Helium	Hydrogen	Nitrogen	Oxygen
Atomic Weight			39.948	44.010	4.0026	2.016	28.01	31.999
Normal Boiling Point		°F	-302.6	-109.3	-452.1	-423.0	-320.4	-297.3
Freezing Point		°F	-308.9	-109.3			-346.0	-361.8
Triple Point		°F	-308.9	-69.8		-436.0	-346.0	-361.8
Triple Foliit		psia	10.0	75.2		1.04	1.8	0.022
Critical		°F	-188.1	87.9	-450.3	-399.9	-232.5	-181.1
point		psia	710.0	1071.0	33.2	190.8	493.0	731.4
Density	Gas,	lb/ft³	0.1034	0.1144	0.01034	0.005209	0.07245	0.08281
	NTP							
	Gas, STP	lb/ft³	0.1114	0.1234	0.001114	0.005611	0.05618	0.08921
	Vapor, nbp	lb/ft³	0.363		1.04	0.0831	0.287	0.279
	Liquid, nbp	lb/ft³	86.98	63.35**	7.798	4.428	50.46	71.27
Specific Heat			0.125	0.20	1.25	3.42	0.249	0.220
Specific Heat Ratio			1.67	1.31	1.66	1.42	1.41	1.40
Heat of vaporization		Btu/lb	70.2	246.6*	8.72	191.7	85.6	91.7
Heat of fusion		Btu/lb	12.7	85.6		25.0	11.1	6.0

<sup>\*</sup>Denotes Sublimation temperature at 1 atm \*\*Liquid density at 2 °F and 302 psig

# **Appendix III: Properties of Rando HD Oil Series**

ISO Grade	10	22	32	46	68
Product Number	273252	273276	273277	273278	273279
SDS/MSDS Number USA Colombia El Salvador	23706 — —	23548 — —	23556 33476 33477	23556 33476 33477	23556 33476 33477
AGMA Grade	-	-	_	1	2
API Gravity	27.7	33.7	32.6	31.8	31.6
Viscosity, Kinematic cSt at 40°C cSt at 100°C	10.3 2.5	23.1 4.4	30.4 5.2	43.7 6.5	64.6 8.4
Viscosity, Saybolt SUS at 100°F SUS at 210°F	63 35	120 41	157 44	225 48	334 54
Viscosity Index	48	98	99	97	98
Flash Point, °C(°F)	154(309)	177(351)	220(428)	226(439)	235(455)
Pour Point, °C(°F)	-39(-38)	-36(-33)	-33(-27)	-30(-22)	-30(-22)
Oxidation Stability Hours to 2.0 mg KOH/g acid number, ASTM D943	_	_	>5000	>5000	>5000

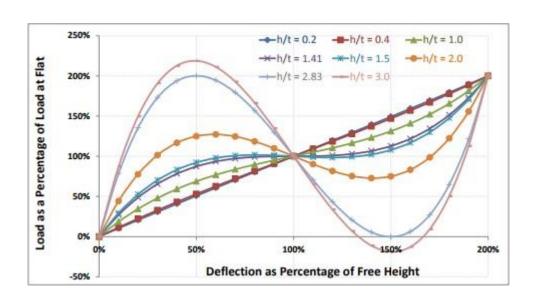
## **Appendix IV: MATLAB Code for vibrational analysis**

```
$_____
응
%Program2.m
%Program for calling the subroutine FREVIB
%Run "Program2" in MATLAB Command Window. Program2.m and frevib.m
%should be in the same file folder, and set the path to this folder
%following 7 lines contain problem-dependent data
m=250;
k=32476.46;
c=2301.09;
x0=0.11;
xd0=1.144;
n=100;
delt=0.025;
%end of problem-dependent data
[x,xd,xdd,t,ii]=FREVIB(m,k,c,x0,xd0,n,delt);
fprintf('Free vibration analysis \n');
fprintf('of a single degree of freedom analysis \n\n');
fprintf('Data:\n\n');
fprintf('m=
              %8.8e \n',m);
fprintf('k=
              %8.8e \n',k);
fprintf('c=
              %8.8e \n',c);
fprintf('x0=
              %8.8e \n',x0);
fprintf('xd0=
              %8.8e \n',xd0);
fprintf('n= %2.0f \n',n);
fprintf('delt= %8.8e \n\n\n',delt);
if ii==1
  fprintf('system is undamped \n\n');
elseif ii==2
  fprintf('system is under damped \n');
elseif ii==3
  fprintf('system is critically damped \n');
  fprintf('system is over damped \n\n');
fprintf('Results:\n\n');
fprintf(' i time(i)
                              x(i)
                                            xd(i)
                                                           xdd(i)');
fprintf('\n\n');
for i=1:100
  fprintf('%2.0f %8.6e %8.6e %8.6e \n',i,t(i),x(i),...
      xd(i), xdd(i);
end
plot(t,x);
hold on;
gtext('x(t)');
plot(t,xd);
gtext('xd(t)');
plot(t,xdd);
gtext('xdd(t)');
xlabel('t');
ylabel('x(t), xd(t), xdd(t)');
title('Vibration analysis viscously damped vibration system');
```

```
용
%Subroutine frevib.m
function [x,xd,xdd,t,ii]=frevib(m,k,c,x0,xd0,n,delt);
omn=sqrt(k/m);
%undamped system
if (abs(c) > 1.0e-6)
  ccrit=2.0*sqrt(k*m);
  xai=c/ccrit;
  if xai<1.0
     %Underdamped system
     ii=2;
     omd=sqrt(1.0-(xai^2))*omn;
     cp1=x0;
     cp2=(xd0+xai*omn*x0)/omd;
     a=sqrt(cp1^2+cp2^2);
     phi=atan(cp1/cp2);
     for i=1:n
        if i>1
           t(i)=t(i-1)+delt;
        else
           t(i)=delt;
        end
        tt=t(i);
        x(i) = a \cdot exp(-xai \cdot omn \cdot tt) \cdot sin(omd \cdot tt + phi);
        xd(i) = a*exp(-xai*omn*tt)*(omd*cos(omd*tt+phi)-xai*omn*...
            sin(omd*tt+phi));
        xdd(i) = -(c*xd(i)+k*x(i))/m;
     end
  elseif xai==1.0
     %critically damped system
     ii=3;
     for i=1:n
        if i>1
           t(i)=t(i-1)+delt;
        else
           t(i) = delt;
        end
        tt=t(i);
        x(i) = (x0+(xd0+omn*x0)*tt)*exp(-omn*tt);
        xd(i) = -(x0+(xd0+omn*x0)*tt)*omn*exp(-omn*tt)+(xd0+omn*x0)*...
            exp(-omn*tt);
        xdd(i) = -(c*xd(i)+k*x(i))/m;
     end
  elseif xai>0
     %overdamped system
     ii=4;
     x1=sqrt(xai^2-1.0);
     c1=(x0*omn*(xai+x1)+xd0)/(2.0*omn*x1);
     c2=(-x0*omn*(xai-x1)-xd0)/(2.0*omn*x1);
     for i=1:n
        if i>1
           t(i)=t(i-1)+delt;
        else
           t(i) = delt;
        end
        tt=t(i);
```

```
x(i) = c1 \cdot exp((-xai + x1) \cdot omn \cdot tt) + c2 \cdot exp((-xai - x1) \cdot omn \cdot tt);
          xd(i)=c1*(-xai+x1)*omn*exp((-xai+x1)*omn*tt)
          +c2*(-xai-x1)*omn*exp((-xai-x1)*omn*tt);
          xdd(i) = -(c*xd(i)+k*x(i))/m;
       end
   end
else
   ii=1;
   omn=sqrt(k/m);
   a = sqrt(x0^2 + (xd0/omn)^2);
   phi=atan(xd0/(x0*omn));
   for i=1:n
       if i>1
          t(i)=t(i-1)+delt;
       else
          t(i)=delt;
       end
       tt=t(i);
       x(i) = a * cos(omn*tt-phi);
       xd(i) = a*omn*cos(omn*tt-phi+1.5708);
      xdd(i) = -(c*xd(i)+k*x(i))/m;
   end
end
```

# Appendix V: h/t ratio graph for shim equations



## **Appendix VI: Accelerometer readings of old damper**

```
# Accelerometer Data File
# Started @Tue Nov 28 15:43:04 GMT+05:00 2017
# sensor Vendor: Invensense
# sensor Name: MPU6500 Acceleration Sensor
# sensor Resolution: 0.0011971008m/sec^2; Max Range: 39.2266; Min Delay: 5000
microseconds
# The sensor's attributes are the result hardware and the Android
capabilities.
# It means that the Android may not utilize all features provided by the
# Some devices and Android versions save battery too much so the device may
go to sleep.
# It just happens after couple of minutes from turning off the scree and it
is easy to find it out.
\# The following file provides the data from accelerometer in the m/s^2
# The diff value is just a time delta between the samples
# data format:
\# so we have 4 columns with values separated by the " "
# X Y Z time from previous sample(ms)
# sensor speed set to:NORMAL
# units set to: m/sec^2
# gravity NOT filtered out
# Accuracy: HIGH
```

Data	Acceleration	Velocity	Displacement
10.758	0.290106192	0.000362633	4.53291E-07
10.152	0.124739715	0.001399748	4.85924E-06
8.979	-0.195350841	0.00122322	1.14167E-05
8.664	-0.281308663	3.15709E-05	1.45536E-05
10.277	0.158849962	-0.000274576	1.39461E-05
8.513	-0.322513841	-0.000683736	1.15503E-05
8.074	-0.442309028	-0.002595793	3.35152E-06
12.119	0.661498559	-0.002047819	-8.2575E-06
12.063	0.646217168	0.00122147	-1.03234E-05
13.093	0.927285602	0.005155227	5.61837E-06
15.649	1.624771929	0.011535371	4.73449E-05
6.123	-0.974701761	0.013160547	0.000109085
6.375	-0.905935503	0.008458953	0.000163133
11.15	0.397075926	0.007186805	0.000202248
16.47	1.848808031	0.012801514	0.000252219
6.91	-0.759943647	0.015523675	0.000323032

7.498	-0.599489046	0.012125094	0.000392153
7.41	-0.623502659	0.009067614	0.000445135
7.164	-0.690631625	0.005782279	0.00048226
15.94	1.704180584	0.008316151	0.000517506
13.549	1.051719783	0.015205902	0.000576311
14.001	1.175062435	0.020772858	0.000666258
11.619	0.525057572	0.025023158	0.000780748
5.936	-1.02573069	0.023771475	0.000902735
7.808	-0.514895634	0.019919909	0.001011963
8.935	-0.207357648	0.018114276	0.001107049
7.339	-0.64287728	0.015988688	0.001192306
10.642	0.258451883	0.015027625	0.001269847
12.546	0.778019162	0.017618803	0.001351463
10.688	0.271004453	0.020241362	0.001446113
13.998	1.174243789	0.023854482	0.001556353
10.101	0.110822734	0.027067148	0.001683657
7.317	-0.648880683	0.025722004	0.00181563
15.819	1.671161865	0.028277707	0.001950629
14.213	1.232913414	0.035537895	0.002110168
9.299	-0.108028609	0.038350107	0.002294888
6.56	-0.855452338	0.035941404	0.002480617
13.255	0.971492482	0.036231505	0.002661049
12.187	0.680054533	0.040360372	0.002852529
11.354	0.452743848	0.043192368	0.003061411
5.471	-1.152620808	0.041442676	0.003272998
11.101	0.383704709	0.039520386	0.003475406
14.616	1.34288485	0.04383686	0.003683799
9.032	-0.180888097	0.046741851	0.003910246
11.796	0.573357681	0.047723025	0.004146408
12.425	0.745000443	0.051018921	0.004393263
10.31	0.167855067	0.053301059	0.004654063
7.293	-0.655429851	0.052082122	0.004917521
8.443	-0.34161558	0.049589509	0.0051717
9.275	-0.114577777	0.048449026	0.005416796
12.999	0.901634697	0.050416668	0.005663961
9.755	0.016405571	0.052711768	0.005921782
9.07	-0.170518582	0.052326486	0.006184377
10.875	0.322033383	0.052705273	0.006446957
12.288	0.707615613	0.055279395	0.006716918
4.847	-1.32289916	0.053741187	0.00698947
7.313	-0.649972211	0.048809008	0.007245845
17.697	2.183634214	0.052643163	0.007499476
6.321	-0.92067113	0.055800571	0.007770585

14.714	1.369627283	0.056922961	0.008052394
5.633	-1.108413928	0.057575995	0.008338641
2.176	-2.051766915	0.049675543	0.00860677
10.168	0.129105827	0.04486889	0.008843131
4.217	-1.494814804	0.041454617	0.00905894
11.134	0.392709814	0.038699355	0.009259325
10.972	0.348502934	0.040552387	0.009457454
11.948	0.614835741	0.042960733	0.009666237
4.031	-1.545570852	0.040633896	0.009875224
14.574	1.331423807	0.040098528	0.010077055
4.599	-1.39057389	0.039950653	0.010277178
9.769	0.020225919	0.036524783	0.010468366
17.761	2.20109866	0.042078094	0.010664873
6.451	-0.885196473	0.04536785	0.010883488
17.167	2.039006767	0.048252376	0.011117539
1.084	-2.349754031	0.047475507	0.011356859
14.938	1.430752846	0.045178004	0.011588492
4.769	-1.344183954	0.045394427	0.011814923
14.071	1.194164174	0.045019377	0.012040958
7.872	-0.497431187	0.04676121	0.012270409
15.176	1.495698755	0.049256879	0.012510455
5.847	-1.050017186	0.050371083	0.012759524
13.193	0.9545738	0.050132474	0.013010783
12.051	0.642942585	0.054126265	0.01327143
14.682	1.36089506	0.059135859	0.013554586
9.578	-0.031894538	0.06245836	0.013858571
1.183	-2.322738715	0.056571777	0.014156146
4.51	-1.414860386	0.04722778	0.014415645
6.671	-0.825162439	0.041627722	0.014637784
14.214	1.233186296	0.042647782	0.014848473
17.122	2.026727078	0.050797566	0.015082086
4.432	-1.43614518	0.05227402	0.015339765
4.426	-1.437782472	0.045089201	0.015583173
4.112	-1.523467412	0.037686076	0.015790111
4.566	-1.399578995	0.03037846	0.015960273
9.503	-0.052360687	0.026748611	0.01610309
4.343	-1.460431676	0.02296663	0.016227379
8.271	-0.388551279	0.018344173	0.016330656
8.242	-0.396464857	0.016381633	0.01641747
9.15	-0.148688024	0.01501875	0.016495971
6.404	-0.898021926	0.012401976	0.016564523
6.552	-0.857635394	0.008012832	0.01661556
12.976	0.895358411	0.00810714	0.01665586

11.337	0.448104855	0.011465798	0.016704792
8.422	-0.347346101	0.011717695	0.016762751
7.977	-0.46877858	0.009677383	0.016816239
7.565	-0.581205953	0.007052422	0.016858063
7.775	-0.523900739	0.004289655	0.016886418
11.75	0.56080511	0.004381916	0.016908097
7.495	-0.600307692	0.00428316	0.01692976
9.929	0.063887035	0.002942108	0.016947823
7.797	-0.517897335	0.001807082	0.016959696
10.933	0.337860537	0.00135699	0.016967606
11.162	0.400350509	0.003202518	0.016979005
8.101	-0.434941215	0.003116041	0.016994801
8.58	-0.304230749	0.001268111	0.017005762
9.17	-0.143230384	0.000149458	0.017009306
9.582	-0.030803011	-0.000285625	0.017008965

<sup>#</sup> Completed @Tue Nov 28 15:43:26 GMT+05:00 2017

## Appendix VII: Accelerometer readings for new damper at 1 bar

```
# Accelerometer Data File
# Started @Mon May 07 12:00:06 GMT+05:00 2018
# sensor Vendor: Invensense
# sensor Name: MPU6500 Acceleration Sensor
# sensor Resolution: 0.0011971008m/sec^2; Max Range: 39.2266; Min Delay: 5000
microseconds
# The sensor's attributes are the result hardware and the Android
capabilities.
# It means that the Android may not utilize all features provided by the
# Some devices and Android versions save battery too much so the device may
go to sleep.
# It just happens after couple of minutes from turning off the scree and it
is easy to find it out.
\# The following file provides the data from accelerometer in the m/s^2
# The diff value is just a time delta between the samples
# data format:
\# so we have 4 columns with values separated by the " "
# X Y Z time from previous sample(ms)
# sensor speed set to:NORMAL
# units set to: m/sec^2
# gravity NOT filtered out
# Accuracy: HIGH
```

# Accuracy	• 111-011		
Data	Acceleration	Velocity	Displacement
9.406	-0.16199664	-0.00162	-1.61997E-05
9.707	0.000137449	0.18951	0.001862701
9.674	-0.01763805	0.38332	0.007591002
9.904	0.106251785	0.5791	0.017215202
9.78	0.039459005	0.77594	0.030765603
9.752	0.024376764	0.97126	0.048237604
9.485	-0.11944317	1.16363	0.069586504
9.712	0.002830706	1.3556	0.094778805
9.394	-0.16846046	1.54666	0.123801406
9.179	-0.28427052	1.73239	0.156591906
9.373	-0.17977214	1.91791	0.193094907
9.56	-0.07904431	2.10724	0.233346408
9.902	0.105174482	2.30186	0.277437408
9.66	-0.02517917	2.49748	0.325430809
9.752	0.024376764	2.6916	0.37732161
9.671	-0.019254	2.88583	0.43309591

9.598	-0.05857556	3.07852	0.492739411
9.69	-0.00901963	3.2714	0.556238612
11.022	0.708464111	3.47852	0.623737812
10.293	0.315787201	3.69167	0.695439713
10.536	0.446679504	3.89996	0.771356014
10.052	0.185972201	4.10584	0.851414014
10.099	0.211288819	4.30735	0.935545915
9.756	0.02653137	4.5059	1.023678416
9.433	-0.14745305	4.69779	1.115715316
9.339	-0.19808629	4.88551	1.211548317
11.493	0.962168945	5.09383	1.311341718
15.258	2.990191669	5.36134	1.415893418
10.845	0.613122803	5.62237	1.525730519
9.12	-0.31605095	5.82202	1.64017442
10.982	0.686918053	6.02304	1.758625021
10.243	0.288854628	6.23529	1.881208321
9.045	-0.35644981	6.42817	2.007842922
9.817	0.059389109	6.61679	2.138292523
10.824	0.601811123	6.8232	2.272692423
9.792	0.045922823	7.02936	2.411218024
8.397	-0.70549596	7.21125	2.553624125
7.74	-1.05938996	7.37262	2.699462825
10.912	0.649212451	7.55914	2.848780426
11.652	1.047814527	7.78478	3.002219627
10.159	0.243607906	8.00289	3.160096327
10.915	0.650828405	8.21363	3.322261528
6.236	-1.86952175	8.38514	3.488249229
9.306	-0.21586178	8.54056	3.657506229
9.879	0.092785499	8.73241	3.83023593
8.878	-0.44640461	8.91998	4.006759831
10.21	0.27107913	9.11086	4.187068231
9.167	-0.29073434	9.30463	4.371223132
9.475	-0.12482969	9.49105	4.559179933
11.261	0.837201808	9.69841	4.751074533
10.776	0.575955853	9.91878	4.947246434
12.41	1.456112329	10.15064	5.147940635
10.828	0.603965729	10.38302	5.353277235
9.428	-0.15014631	10.58558	5.562963236
11.529	0.981560398	10.79515	5.776770537
12.051	1.262736457	11.03095	5.995031537
8.81	-0.48303291	11.23956	6.217736638
12.873	1.705507952	11.45639	6.444696139
9.981	0.147727947	11.68493	6.676109339

11.037	0.716543882	11.89511	6.91190974
10.68	0.524245313	12.11228	7.151983641
9.896	0.101942574	12.31804	7.396286841
9.005	-0.37799587	12.50705	7.644537742
10.65	0.50808577	12.7036	7.896644243
10.177	0.253303632	12.91187	8.152798943
9.324	-0.20616606	13.10688	8.412986444
10.093	0.20805691	13.30105	8.677065745
9.06	-0.34837004	13.49258	8.945002045
10.534	0.445602201	13.68852	9.216813046
9.591	-0.06234612	13.88977	9.492595947
8.052	-0.89133071	14.0662	9.772155647
8.202	-0.81053299	14.22874	10.05510505
9.64	-0.0359522	14.40716	10.34146405
9.348	-0.19323842	14.59704	10.63150605
8.881	-0.44478865	14.77933	10.92526975
10.168	0.248455769	14.96982	11.22276125
9.902	0.105174482	15.17052	11.52416465
10.232	0.282929462	15.37186	11.82958845
8.878	-0.44640461	15.56296	12.13893665
10.016	0.166580748	15.7519	12.45208525
8.355	-0.72811932	15.93561	12.76896035
11.036	0.716005231	16.12952	13.08961165
10.353	0.348106288	16.34341	13.41434096
9.803	0.051847989	16.54497	13.74322476
9.288	-0.22555751	16.73588	14.07603326
11.013	0.703616248	16.93889	14.41278096
9.026	-0.36668419	17.13928	14.75356266
9.742	0.01899025	17.32696	15.09822506
11.337	0.878139319	17.53775	15.44687216
10.684	0.526399919	17.75796	15.79982926
8.401	-0.70334135	17.94881	16.15689696
9.313	-0.21209122	18.12595	16.51764456
10.386	0.365881786	18.32294	16.88213346
11.02	0.707386808	18.537	17.25073286
10.229	0.281313508	18.74949	17.62359776
9.206	-0.26972693	18.94384	18.00053106
9.775	0.036765748	19.13365	18.38130596
8.683	-0.55144164	19.31823	18.76582477
10.517	0.436445127	19.51023	19.15410937
10.481	0.417053674	19.72021	19.54641377
8.738	-0.52181581	19.9124	19.94273987
10.916	0.651367057	20.10894	20.34295327

9.394	-0.16846046	20.31204	20.74716307
10.087	0.204825001	20.50685	21.15535197
9.604	-0.05534365	20.70376	21.56745807
9.554	-0.08227622	20.89534	21.98344907
11.817	1.136692016	21.10905	22.40349297
9.864	0.084705727	21.32586	22.82784207
8.367	-0.7216555	21.50817	23.25618237
7.481	-1.19890069	21.66665	23.68793057
10.071	0.196206578	21.84217	24.12301877
10.235	0.284545417	22.04523	24.56189277
9.901	0.104635831	22.24659	25.00481098
9.988	0.151498507	22.44548	25.45173168
9.534	-0.09304925	22.6407	25.90259348
9.2	-0.27295884	22.82804	26.35728088
9.771	0.034611142	23.01775	26.81573878
9.728	0.01144913	23.21274	27.27804368
9.575	-0.07096454	23.40577	27.74422878
9.514	-0.10382228	23.59666	28.21425308
9.246	-0.24818087	23.78426	28.68806228
8.76	-0.50996548	23.96432	29.16554808
10.315	0.327637533	24.15507	29.64674198
9.646	-0.03272029	24.35468	30.13183948
8.966	-0.39900328	24.5408	30.62079428
9.703	-0.00201716	24.72749	31.11347718
8.941	-0.41246956	24.91393	31.60989139
8.07	-0.88163498	25.08404	32.10987109
13.113	1.8347843	25.29587	32.61367019
9.616	-0.04887983	25.52316	33.12186049
6.684	-1.6282059	25.68616	33.63395369
12.01	1.240651747	25.8731	34.14954629
11.344	0.881909879	26.10664	34.66934369
10.546	0.452066019	26.32554	35.19366549
8.995	-0.38338239	26.52095	35.72213039
9.743	0.019528901	26.70833	36.25442319
11.273	0.843665626	26.91849	36.79069139
9.963	0.138032221	27.13085	37.33118479
10.104	0.213982076	27.33152	37.87580849
9.245	-0.24871952	27.52501	38.42437379
9.568	-0.0747351	27.71314	38.97675529
9.497	-0.11297936	27.90379	39.5329246
10.028	0.173044566	28.09904	40.0929529
11.548	0.991794775	28.3148	40.6570913
6.714	-1.61204635	28.49742	41.2252135

12.3	1.396860669	28.68756	41.7970633
5.063	-2.5013599	28.86119	42.3725508
5.45	-2.29290179	28.96632	42.9508259
13.074	1.813776894	29.15156	43.5320047
9.265	-0.23794649	29.37495	44.1172698
11.639	1.040812058	29.58399	44.7068592
10.08	0.201054441	29.80118	45.3007109
5.826	-2.09036884	29.96024	45.8983251
9.721	0.007678569	30.11571	46.4990846
9.786	0.042690914	30.31078	47.1033495
11.99	1.229878718	30.52854	47.7117427
9.701	-0.00309446	30.74545	48.32448261
6.607	-1.66968206	30.90853	48.94102241
8.128	-0.8503932	31.05588	49.56066651
10.437	0.39335301	31.24153	50.18364061
6.112	-1.93631453	31.40702	50.81012611
6.044	-1.97294283	31.52858	51.43948211
9.983	0.14880525	31.68885	52.07165641
11.251	0.831815294	31.90119	52.70755681
10.05	0.184894898	32.1142	53.34771071
11.626	1.033809589	32.33096	53.99216231
11.631	1.036502846	32.56353	54.64110721
8.695	-0.54497782	32.76679	55.29441041
9.783	0.041074959	32.95157	55.95159401
12.032	1.252502079	33.16972	56.61280691
6.375	-1.79464919	33.35379	57.27804201
8.992	-0.38499834	33.50746	57.94665452
10.923	0.655137617	33.70661	58.61879522
7.229	-1.33464085	33.88813	59.29474262
11.911	1.187325253	34.07953	59.97441922
11.2	0.804344069	34.31064	60.65832092
7.478	-1.20051664	34.49742	61.34640152
11.178	0.792493737	34.68398	62.03821552
6.545	-1.70307845	34.86121	62.73366742
11.104	0.75263353	35.0377	63.43265652
5.943	-2.02734662	35.20817	64.13511522
6.566	-1.69176677	35.33326	64.84052952
10.809	0.593731351	35.50701	65.54893222
12.228	1.358077764	35.73738	66.26137612
9.069	-0.34352218	35.95035	66.97825342
10.295	0.316864504	36.14399	67.69919682
5.368	-2.33707121	36.30062	68.42364293
6.169	-1.90561139	36.41599	69.15080903

8.979	-0.39200081	36.56747	69.88064363
13.593	2.093336998	36.79319	70.61425023
11.18	0.79357104	37.04092	71.35259133
8.961	-0.40169654	37.24233	72.09542383
10.287	0.312555292	37.43481	72.84219523
11.961	1.214257826	37.65729	73.59311623
9.041	-0.35860442	37.86731	74.34836223
13.165	1.862794176	38.08937	75.10792903
10.432	0.390659753	38.32534	75.87207613
12.666	1.594007101	38.55632	76.64089273
12.18	1.332222494	38.80478	77.41450373
12.465	1.485738158	39.05123	78.19306383
11.063	0.73054882	39.28651	78.97644123
10.174	0.251687678	39.49888	79.76429514
8.439	-0.68287259	39.68501	80.55613404
6.852	-1.53771245	39.83792	81.35136334
11.081	0.740244546	40.01725	82.14991504
5.05	-2.50836237	40.17856	82.95187314
8.418	-0.69418427	40.31324	83.75679114
7.376	-1.25545909	40.47118	84.56463534
11.253	0.832892597	40.65747	85.37592184
8.052	-0.89133071	40.85052	86.19100174
8.457	-0.67317687	41.01561	87.00966304
11.803	1.129150896	41.21821	87.83200124
12.152	1.317140253	41.45776	88.65876094
11.214	0.81188519	41.69142	89.49025274
9.418	-0.15553282	41.89774	90.32614434
9.023	-0.36830015	42.08215	91.16594324
9.812	0.056695852	42.2705	92.00946975
10.086	0.20428635	42.46948	92.85686955
11.137	0.770409028	42.68171	93.70838145
7.36	-1.26407751	42.86668	94.56386535
11.083	0.741321849	43.05111	95.42304325
2.309	-3.98480601	43.18503	96.28540465
-3.011	-6.85043174	43.17801	97.14903505
19.567	5.311240783	43.34357	98.01425085
11.273	0.843665626	43.65197	98.88420625
8.173	-0.82615388	43.84643	99.75919025
9.398	-0.16630585	44.02214	100.637876
8.1	-0.86547544	44.19712	101.5200686
10.626	0.495158135	44.38438	102.4058836
6.758	-1.58834569	44.55822	103.2953096
5.918	-2.04081291	44.68498	104.1877416

7.521         -1.17735463         44.81937         105.0827851           8.231         -0.7949121         44.97689         105.9807477           12.691         1.607473387         45.18611         106.8823777           7.517         -1.17950923         45.38819         107.7881207           5.972         -2.01172573         45.52308         108.6972334           10.976         0.683686144         45.69256         109.6093898           9.527         -0.09681981         45.89759         110.5252913           9.707         0.000137449         46.08993         111.4451665           8.724         -0.52935693         46.27424         112.3688082           9.441         -0.14314384         46.45589         113.2961095           10.676         0.522090708         46.65706         114.227239           13.511         2.049167579         46.89893         115.1627989           8.057         -0.88863745         47.11461         116.1029343           9.885         0.096017408         47.29403         117.0470207           10.888         0.63284816         47.50176         117.9949786           10.467         0.409512554         47.71531         18.9474493           11.05				
12.691         1.607473387         45.18611         106.8823777           7.517         -1.17950923         45.38819         107.7881207           5.972         -2.01172573         45.52308         108.6972334           10.976         0.683686144         45.69256         109.6093898           9.527         -0.09681981         45.89759         110.5252913           9.707         0.000137449         46.08993         111.4451665           8.724         -0.52935693         46.27424         112.3688082           9.441         -0.14314384         46.45589         113.2961095           10.676         0.522090708         46.65706         114.227239           13.511         2.049167579         46.89893         115.1627989           8.057         -0.88863745         47.11461         116.1029343           9.885         0.096017408         47.29403         117.0470207           10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10	7.521	-1.17735463	44.81937	105.0827851
7.517 -1.17950923 45.38819 107.7881207 5.972 -2.01172573 45.52308 108.6972334 10.976 0.683686144 45.69256 109.6093898 9.527 -0.09681981 45.89759 110.5252913 9.707 0.000137449 46.08993 111.4451665 8.724 -0.52935693 46.27424 112.3688082 9.441 -0.14314384 46.45589 113.2961095 10.676 0.522090708 46.65706 114.227239 13.511 2.049167579 46.89893 115.1627989 8.057 -0.88863745 47.11461 116.1029343 9.885 0.096017408 47.29403 117.0470207 10.888 0.636284816 47.50176 117.9949786 10.467 0.409512554 47.71531 118.9471493 11.055 0.726239609 47.93053 119.9036077 8.74 -0.52073851 48.12848 120.8641978 10.238 0.286161371 48.31826 121.8286652 9.186 -0.28049996 48.5125 122.7969728 9.877 0.091708196 48.70313 123.7691291 9.783 0.041074959 48.89973 124.7451577 10.066 0.193513321 49.09822 125.7251372 8.444 -0.68017934 49.28332 126.7089526 10.599 0.480614546 49.47375 127.6965233 10.314 0.327098881 49.68288 128.6880896 8.677 -0.55467355 49.87279 129.6836463 8.257 -0.78090716 50.04213 130.6827955 10.413 0.380425375 50.22883 131.6855051 10.115 0.219907242 50.43411 132.6921345 9.873 0.08955359 50.63399 133.7028155 10.419 0.383657284 50.83691 134.7175245 9.9764 0.030840582 51.03874 135.736281 9.543 -0.08820139 51.23181 136.7589865 9.939 0.125104586 51.42663 137.7855709 10.66 0.513472284 51.63262 138.8161634 10.146 0.236605437 51.84068 139.8508964 10.075 0.198361184 52.04289 144.0303515 8.95 -0.4076217 52.84956 145.08534	8.231	-0.7949121	44.97689	105.9807477
5.972         -2.01172573         45.52308         108.6972334           10.976         0.683686144         45.69256         109.6093898           9.527         -0.09681981         45.89759         110.5252913           9.707         0.000137449         46.08993         111.4451665           8.724         -0.52935693         46.27424         112.3688082           9.441         -0.14314384         46.45589         113.2961095           10.676         0.522090708         46.65706         114.227239           13.511         2.049167579         46.89893         115.1627989           8.057         -0.88863745         47.11461         116.1029343           9.885         0.096017408         47.29403         117.0470207           10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.8		1.607473387	45.18611	106.8823777
10.976         0.683686144         45.69256         109.6093898           9.527         -0.09681981         45.89759         110.5252913           9.707         0.000137449         46.08993         111.4451665           8.724         -0.52935693         46.27424         112.3688082           9.441         -0.14314384         46.45589         113.2961095           10.676         0.522090708         46.65706         114.227239           13.511         2.049167579         46.89893         115.1627989           8.057         -0.88863745         47.11461         116.1029343           9.885         0.096017408         47.29403         117.0470207           10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.7	7.517	-1.17950923	45.38819	107.7881207
9.527 -0.09681981 45.89759 110.5252913 9.707 0.000137449 46.08993 111.4451665 8.724 -0.52935693 46.27424 112.3688082 9.441 -0.14314384 46.45589 113.2961095 10.676 0.522090708 46.65706 114.227239 13.511 2.049167579 46.89893 115.1627989 8.057 -0.88863745 47.11461 116.1029343 9.885 0.096017408 47.29403 117.0470207 10.888 0.636284816 47.50176 117.9949786 10.467 0.409512554 47.71531 118.9471493 11.055 0.726239609 47.93053 119.9036077 8.74 -0.52073851 48.12848 120.8641978 10.238 0.286161371 48.31826 121.8286652 9.186 -0.28049996 48.5125 122.7969728 9.877 0.091708196 48.70313 123.7691291 9.783 0.041074959 48.89973 124.7451577 10.066 0.193513321 49.09822 125.7251372 8.444 -0.68017934 49.28332 126.7089526 10.599 0.480614546 49.47375 127.6965233 10.314 0.327098881 49.68288 128.6880896 8.677 -0.55467355 49.87279 129.6836463 8.257 -0.78090716 50.04213 130.6827955 10.413 0.380425375 50.22883 131.6855051 10.115 0.219907242 50.43411 132.6921345 9.873 0.08955359 50.63399 133.7028155 10.419 0.383657284 50.83691 134.7175245 9.764 0.030840582 51.03874 135.736281 9.543 -0.08820139 51.23181 136.7589865 9.939 0.125104586 51.42663 137.7855709 10.66 0.513472284 51.63262 138.8161634 10.146 0.236605437 51.84068 139.8508964 10.075 0.198361184 52.04289 140.8897321 10.008 0.162271537 52.24372 141.9325982 9.736 0.015758341 52.44116 142.979447 11.077 0.738089941 52.64929 144.0303515 8.95 -0.4076217 52.84956 145.08534	5.972	-2.01172573	45.52308	108.6972334
9.707         0.000137449         46.08993         111.4451665           8.724         -0.52935693         46.27424         112.3688082           9.441         -0.14314384         46.45589         113.2961095           10.676         0.522090708         46.65706         114.227239           13.511         2.049167579         46.89893         115.1627989           8.057         -0.88863745         47.11461         116.1029343           9.885         0.096017408         47.29403         117.0470207           10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.4		0.683686144	45.69256	109.6093898
8.724       -0.52935693       46.27424       112.3688082         9.441       -0.14314384       46.45589       113.2961095         10.676       0.522090708       46.65706       114.227239         13.511       2.049167579       46.89893       115.1627989         8.057       -0.88863745       47.11461       116.1029343         9.885       0.096017408       47.29403       117.0470207         10.888       0.636284816       47.50176       117.9949786         10.467       0.409512554       47.71531       118.9471493         11.055       0.726239609       47.93053       119.9036077         8.74       -0.52073851       48.12848       120.8641978         10.238       0.286161371       48.31826       121.8286652         9.186       -0.28049996       48.5125       122.7969728         9.877       0.091708196       48.70313       123.7691291         9.783       0.041074959       48.89973       124.7451577         10.066       0.193513321       49.09822       125.7251372         8.444       -0.68017934       49.28332       126.7089526         10.599       0.480614546       49.47375       127.6965233         10.3	9.527	-0.09681981	45.89759	110.5252913
9.441         -0.14314384         46.45589         113.2961095           10.676         0.522090708         46.65706         114.227239           13.511         2.049167579         46.89893         115.1627989           8.057         -0.88863745         47.11461         116.1029343           9.885         0.096017408         47.29403         117.0470207           10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10	9.707	0.000137449	46.08993	111.4451665
10.676         0.522090708         46.65706         114.227239           13.511         2.049167579         46.89893         115.1627989           8.057         -0.88863745         47.11461         116.1029343           9.885         0.096017408         47.29403         117.0470207           10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.32709881         49.68288         128.688089           8.6	8.724	-0.52935693	46.27424	112.3688082
13.511       2.049167579       46.89893       115.1627989         8.057       -0.88863745       47.11461       116.1029343         9.885       0.096017408       47.29403       117.0470207         10.888       0.636284816       47.50176       117.9949786         10.467       0.409512554       47.71531       118.9471493         11.055       0.726239609       47.93053       119.9036077         8.74       -0.52073851       48.12848       120.8641978         10.238       0.286161371       48.31826       121.8286652         9.186       -0.28049996       48.5125       122.7969728         9.877       0.091708196       48.70313       123.7691291         9.783       0.041074959       48.89973       124.7451577         10.066       0.193513321       49.09822       125.7251372         8.444       -0.68017934       49.28332       126.7089526         10.599       0.480614546       49.47375       127.6965233         10.314       0.32709881       49.68288       128.6880896         8.677       -0.755467355       49.87279       129.6836463         8.257       -0.78090716       50.04213       130.6827955         10.		-0.14314384	46.45589	113.2961095
8.057         -0.88863745         47.11461         116.1029343           9.885         0.096017408         47.29403         117.0470207           10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.327098881         49.68288         128.6880896           8.677         -0.55467355         49.87279         129.6836463           8.257         -0.78090716         50.04213         130.6827955           10		0.522090708	46.65706	114.227239
9.885         0.096017408         47.29403         117.0470207           10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.327098881         49.87279         129.6836463           8.257         -0.78090716         50.04213         130.6827955           10.413         0.380425375         50.22883         131.6855051           10.115         0.219907242         50.43411         132.6921345		2.049167579	46.89893	115.1627989
10.888         0.636284816         47.50176         117.9949786           10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.327098881         49.68288         128.6880896           8.677         -0.55467355         49.87279         129.6836463           8.257         -0.78090716         50.04213         130.6827955           10.413         0.380425375         50.22883         131.6855051           10.15         0.219907242         50.43411         132.6921345           9	8.057	-0.88863745	47.11461	116.1029343
10.467         0.409512554         47.71531         118.9471493           11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.327098881         49.68288         128.6880896           8.677         -0.55467355         49.87279         129.6836463           8.257         -0.78090716         50.04213         130.6827955           10.413         0.380425375         50.22883         131.6855051           10.115         0.219907242         50.43411         132.6921345           9.873         0.08955359         50.63399         133.7028155           10	9.885	0.096017408	47.29403	117.0470207
11.055         0.726239609         47.93053         119.9036077           8.74         -0.52073851         48.12848         120.8641978           10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.327098881         49.68288         128.6880896           8.677         -0.55467355         49.87279         129.6836463           8.257         -0.78090716         50.04213         130.6827955           10.413         0.380425375         50.22883         131.6855051           10.115         0.219907242         50.43411         132.6921345           9.873         0.08955359         50.63399         133.702815           10.419         0.383657284         50.83691         134.7175245           9.7		0.636284816	47.50176	117.9949786
8.74       -0.52073851       48.12848       120.8641978         10.238       0.286161371       48.31826       121.8286652         9.186       -0.28049996       48.5125       122.7969728         9.877       0.091708196       48.70313       123.7691291         9.783       0.041074959       48.89973       124.7451577         10.066       0.193513321       49.09822       125.7251372         8.444       -0.68017934       49.28332       126.7089526         10.599       0.480614546       49.47375       127.6965233         10.314       0.327098881       49.68288       128.6880896         8.677       -0.55467355       49.87279       129.6836463         8.257       -0.78090716       50.04213       130.6827955         10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939<		0.409512554	47.71531	118.9471493
10.238         0.286161371         48.31826         121.8286652           9.186         -0.28049996         48.5125         122.7969728           9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.327098881         49.68288         128.6880896           8.677         -0.55467355         49.87279         129.6836463           8.257         -0.78090716         50.04213         130.6827955           10.413         0.380425375         50.22883         131.6855051           10.115         0.219907242         50.43411         132.6921345           9.873         0.08955359         50.63399         133.7028155           10.419         0.383657284         50.83691         134.7175245           9.764         0.030840582         51.03874         135.736281           9.543         -0.08820139         51.23181         136.7589865           9.9	11.055	0.726239609	47.93053	119.9036077
9.186       -0.28049996       48.5125       122.7969728         9.877       0.091708196       48.70313       123.7691291         9.783       0.041074959       48.89973       124.7451577         10.066       0.193513321       49.09822       125.7251372         8.444       -0.68017934       49.28332       126.7089526         10.599       0.480614546       49.47375       127.6965233         10.314       0.327098881       49.68288       128.6880896         8.677       -0.55467355       49.87279       129.6836463         8.257       -0.78090716       50.04213       130.6827955         10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.075		-0.52073851	48.12848	120.8641978
9.877         0.091708196         48.70313         123.7691291           9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.327098881         49.68288         128.6880896           8.677         -0.55467355         49.87279         129.6836463           8.257         -0.78090716         50.04213         130.6827955           10.413         0.380425375         50.22883         131.6855051           10.115         0.219907242         50.43411         132.6921345           9.873         0.08955359         50.63399         133.7028155           10.419         0.383657284         50.83691         134.7175245           9.764         0.030840582         51.03874         135.736281           9.543         -0.08820139         51.23181         136.7589865           9.939         0.125104586         51.42663         137.7855709           10.66         0.513472284         51.63262         138.8161634           10.	10.238	0.286161371	48.31826	121.8286652
9.783         0.041074959         48.89973         124.7451577           10.066         0.193513321         49.09822         125.7251372           8.444         -0.68017934         49.28332         126.7089526           10.599         0.480614546         49.47375         127.6965233           10.314         0.327098881         49.68288         128.6880896           8.677         -0.55467355         49.87279         129.6836463           8.257         -0.78090716         50.04213         130.6827955           10.413         0.380425375         50.22883         131.6855051           10.115         0.219907242         50.43411         132.6921345           9.873         0.08955359         50.63399         133.7028155           10.419         0.383657284         50.83691         134.7175245           9.764         0.030840582         51.03874         135.736281           9.543         -0.08820139         51.23181         136.7589865           9.939         0.125104586         51.42663         137.7855709           10.66         0.513472284         51.63262         138.8161634           10.075         0.198361184         52.04289         140.8897321           10		-0.28049996	48.5125	122.7969728
10.066       0.193513321       49.09822       125.7251372         8.444       -0.68017934       49.28332       126.7089526         10.599       0.480614546       49.47375       127.6965233         10.314       0.327098881       49.68288       128.6880896         8.677       -0.55467355       49.87279       129.6836463         8.257       -0.78090716       50.04213       130.6827955         10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.64929       144.0303515         8.9	9.877	0.091708196	48.70313	123.7691291
8.444       -0.68017934       49.28332       126.7089526         10.599       0.480614546       49.47375       127.6965233         10.314       0.327098881       49.68288       128.6880896         8.677       -0.55467355       49.87279       129.6836463         8.257       -0.78090716       50.04213       130.6827955         10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534		0.041074959	48.89973	124.7451577
10.599       0.480614546       49.47375       127.6965233         10.314       0.327098881       49.68288       128.6880896         8.677       -0.55467355       49.87279       129.6836463         8.257       -0.78090716       50.04213       130.6827955         10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534	10.066	0.193513321	49.09822	125.7251372
10.314       0.327098881       49.68288       128.6880896         8.677       -0.55467355       49.87279       129.6836463         8.257       -0.78090716       50.04213       130.6827955         10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534	8.444	-0.68017934	49.28332	126.7089526
8.677       -0.55467355       49.87279       129.6836463         8.257       -0.78090716       50.04213       130.6827955         10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534		0.480614546	49.47375	127.6965233
8.257       -0.78090716       50.04213       130.6827955         10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534	10.314	0.327098881	49.68288	128.6880896
10.413       0.380425375       50.22883       131.6855051         10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534		-0.55467355	49.87279	129.6836463
10.115       0.219907242       50.43411       132.6921345         9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534	8.257	-0.78090716	50.04213	130.6827955
9.873       0.08955359       50.63399       133.7028155         10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534	10.413	0.380425375	50.22883	131.6855051
10.419       0.383657284       50.83691       134.7175245         9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534	10.115	0.219907242	50.43411	132.6921345
9.764       0.030840582       51.03874       135.736281         9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534	9.873	0.08955359	50.63399	133.7028155
9.543       -0.08820139       51.23181       136.7589865         9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534		0.383657284	50.83691	134.7175245
9.939       0.125104586       51.42663       137.7855709         10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534		0.030840582	51.03874	135.736281
10.66       0.513472284       51.63262       138.8161634         10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534		-0.08820139	51.23181	136.7589865
10.146       0.236605437       51.84068       139.8508964         10.075       0.198361184       52.04289       140.8897321         10.008       0.162271537       52.24372       141.9325982         9.736       0.015758341       52.44116       142.979447         11.077       0.738089941       52.64929       144.0303515         8.95       -0.4076217       52.84956       145.08534		0.125104586	51.42663	137.7855709
10.075     0.198361184     52.04289     140.8897321       10.008     0.162271537     52.24372     141.9325982       9.736     0.015758341     52.44116     142.979447       11.077     0.738089941     52.64929     144.0303515       8.95     -0.4076217     52.84956     145.08534		0.513472284	51.63262	138.8161634
10.008     0.162271537     52.24372     141.9325982       9.736     0.015758341     52.44116     142.979447       11.077     0.738089941     52.64929     144.0303515       8.95     -0.4076217     52.84956     145.08534		0.236605437	51.84068	139.8508964
9.736     0.015758341     52.44116     142.979447       11.077     0.738089941     52.64929     144.0303515       8.95     -0.4076217     52.84956     145.08534	10.075	0.198361184	52.04289	140.8897321
11.077 0.738089941 52.64929 144.0303515 8.95 -0.4076217 52.84956 145.08534		0.162271537	52.24372	141.9325982
8.95 -0.4076217 52.84956 145.08534	9.736	0.015758341	52.44116	142.979447
		0.738089941	52.64929	144.0303515
9.622 -0.04564792 53.03528 146.1441884		-0.4076217	52.84956	145.08534
	9.622	-0.04564792	53.03528	146.1441884

9.521	-0.10005172	53.22671	147.2068083
10.198	0.264615313	53.4239	148.2733144
10.05	0.184894898	53.62638	149.3438172
9.405	-0.16253529	53.82093	150.4182903
10.081	0.201593093	54.01579	151.4966575
9.732	0.013603735	54.21392	152.5789546
8.649	-0.56975579	54.39773	153.6650711
10.143	0.234989483	54.58565	154.7549049
9.297	-0.22070965	54.78005	155.8485619
9.933	0.121872678	54.97235	156.9460859
9.369	-0.18192674	55.16537	158.0474631
8.796	-0.49057403	55.34702	159.152587
8.486	-0.65755598	55.51984	160.2612556
9.824	0.063159669	55.70294	161.3734834
10.34	0.341103819	55.90458	162.4895586
9.773	0.035688445	56.10571	163.6096615

<sup>#</sup> Completed @Mon May 07 12:03:29 GMT+05:00 2018

## **Appendix VIII: Accelerometer readings for new damper at 2 bar**

```
# Accelerometer Data File
# Started @Mon May 07 12:54:27 GMT+05:00 2018
# sensor Vendor: Invensense
# sensor Name: MPU6500 Acceleration Sensor
# sensor Resolution: 0.0011971008m/sec^2; Max Range: 39.2266; Min Delay: 5000
# The sensor's attributes are the result hardware and the Android
capabilities.
# It means that the Android may not utilize all features provided by the
# Some devices and Android versions save battery too much so the device may
go to sleep.
# It just happens after couple of minutes from turning off the scree and it
is easy to find it out.
\# The following file provides the data from accelerometer in the m/s^2
# The diff value is just a time delta between the samples
# data format:
\# so we have 4 columns with values separated by the " "
# X Y Z time from previous sample(ms)
# sensor speed set to:NORMAL
# units set to: m/sec^2
# gravity NOT filtered out
# Accuracy: HIGH
```

# Accura	# Accuracy: HIGH			
Data	Acceleration	Velocity	Displacement	
6.684	-1.06201395	0.002389	5.97246E-06	
12.01	0.955594003	0.002123	1.72523E-05	
11.344	0.703298303	0.00627	3.8235E-05	
10.546	0.40099805	0.009031	7.64877E-05	
8.995	-0.18655545	0.009567	0.000122982	
9.743	0.096803686	0.009343	0.000170257	
11.273	0.676401915	0.011276	0.000221802	
9.963	0.180144608	0.013417	0.000283534	
10.104	0.233558562	0.014451	0.000353205	
9.245	-0.09184986	0.014806	0.000426347	
9.568	0.030509771	0.014652	0.000499991	
9.497	0.003613383	0.014738	0.000573465	
10.028	0.204768062	0.015258	0.000648455	
11.548	0.780578067	0.017722	0.000730906	
6.714	-1.05064928	0.017047	0.000817827	
12.3	1.06545249	0.017084	0.000903153	

5.063	-1.67608501	0.015557	0.000984755
5.45	-1.52948076	0.007543	0.001042505
13.074	1.358661006	0.007116	0.001079153
9.265	-0.08427341	0.010302	0.001122699
11.639	0.815050903	0.012129	0.001178776
10.08	0.224466825	0.014728	0.001245919
5.826	-1.38704354	0.011821	0.001312292
9.721	0.088469594	0.008575	0.001363282
9.786	0.113093048	0.009079	0.001407417
11.99	0.948017555	0.011732	0.001459443
9.701	0.080893146	0.014304	0.001524532
6.607	-1.09118327	0.011778	0.001589737
8.128	-0.51499444	0.007763	0.001638589
10.437	0.359706412	0.007375	0.001676432
6.112	-1.27870035	0.005077	0.001707561
6.044	-1.30446027	-0.00138	0.001716801
9.983	0.187721055	-0.00417	0.001702917
11.251	0.668067822	-0.00203	0.001687402
10.05	0.213102154	0.00017	0.001682743
11.626	0.810126212	0.002728	0.001689987
11.631	0.812020324	0.006783	0.001713764
8.695	-0.30020216	0.008063	0.001750878
9.783	0.111956581	0.007592	0.001790015
12.032	0.963928095	0.010282	0.0018347
6.375	-1.17907006	0.009744	0.001884764
8.992	-0.18769192	0.006327	0.001924941
10.923	0.543814085	0.007217	0.001958802
7.229	-0.85555576	0.006438	0.00199294
11.911	0.918090588	0.006594	0.00202552
11.2	0.648747882	0.010511	0.002068284
7.478	-0.76122899	0.01023	0.002120138
11.178	0.640413789	0.009928	0.002170534
6.545	-1.11467026	0.008742	0.002217211
11.104	0.612380934	0.007487	0.002257784
5.943	-1.34272133	0.005661	0.002290653
6.566	-1.10671499	-0.00046	0.002303649
10.809	0.500628334	-0.00198	0.002297547
12.228	1.03817728	0.001869	0.002297275
9.069	-0.15852259	0.004068	0.002312119
10.295	0.305913635	0.004437	0.002333381
5.368	-1.56054419	0.0013	0.002347723
6.169	-1.25710747	-0.00574	0.002336614
8.979	-0.19261661	-0.00937	0.002298833

13.593	1.555269817	-0.00596	0.002260508
11.18	0.641171434	-0.00047	0.002244428
8.961	-0.19943541	0.000634	0.002244836
10.287	0.302883056	0.000892	0.002248652
11.961	0.937031706	0.003992	0.002260863
9.041	-0.16912962	0.005912	0.002285624
13.165	1.393133842	0.008972	0.002322834
10.432	0.3578123	0.013349	0.002378637
12.666	1.204101478	0.017254	0.002455145
12.18	1.019993806	0.022814	0.002555317
12.465	1.127958182	0.028184	0.002682813
11.063	0.596849217	0.032496	0.002834514
10.174	0.260076128	0.034639	0.003002351
8.439	-0.39718069	0.034296	0.003174687
6.852	-0.99837179	0.030807	0.003337444
11.081	0.603668019	0.02982	0.003489012
5.05	-1.6810097	0.027127	0.003631379
8.418	-0.40513596	0.021911	0.003753975
7.376	-0.79986887	0.018899	0.003856001
11.253	0.668825467	0.018571	0.003949677
8.052	-0.54378494	0.018884	0.004043315
8.457	-0.39036188	0.016549	0.004131896
11.803	0.877177772	0.017766	0.004217682
12.152	1.009386779	0.022482	0.004318301
11.214	0.654051395	0.026641	0.004441107
9.418	-0.02631358	0.02821	0.004578234
9.023	-0.17594842	0.027704	0.004718019
9.812	0.12294243	0.027572	0.004856209
10.086	0.22673976	0.028446	0.004996254
11.137	0.624882072	0.030575	0.005143806
7.36	-0.80593003	0.030122	0.00529555
11.083	0.604425664	0.029619	0.005444903
2.309	-2.71936182	0.024331	0.005579778
-3.011	-4.73469684	0.005696	0.005654847
19.567	3.818354665	0.003405	0.0056776
11.273	0.676401915	0.014642	0.005722719
8.173	-0.49794744	0.015088	0.005797046
9.398	-0.03389003	0.013759	0.005869163
8.1	-0.52560147	0.01236	0.00593446
10.626	0.43130384	0.012124	0.005995671
6.758	-1.03398109	0.010618	0.006052526
5.918	-1.35219189	0.004652	0.0060907
7.521	-0.74493962	-0.00059	0.006100854

-0.47597574	-0.00364	0.00609027
1.213572038	-0.0018	0.006076665
-0.74645491	-0.00063	0.00607059
-1.33173548	-0.00583	0.006054445
0.56389167	-0.00775	0.006020513
0.014978054	-0.0063	0.005985399
0.083166081	-0.00605	0.005954517
-0.28921631	-0.00657	0.005922961
-0.01760067	-0.00734	0.005888199
0.450244959	-0.00625	0.005854223
1.524206382	-0.00132	0.005835292
-0.54189083	0.001138	0.005834841
0.150596463	0.000159	0.005838084
0.530555302	0.001862	0.005843138
0.371071083	0.004116	0.005858084
	1.213572038 -0.74645491 -1.33173548 0.56389167 0.014978054 0.083166081 -0.28921631 -0.01760067 0.450244959 1.524206382 -0.54189083 0.150596463 0.530555302	1.213572038 -0.0018 -0.74645491 -0.00063 -1.33173548 -0.00583 0.56389167 -0.00775 0.014978054 -0.0063 0.083166081 -0.00605 -0.28921631 -0.00657 -0.01760067 -0.00734 0.450244959 -0.00625 1.524206382 -0.00132 -0.54189083 0.001138 0.150596463 0.000159 0.530555302 0.001862

<sup>#</sup> Completed @Mon May 07 12:56:02 GMT+05:00 2018

## Appendix IX: Accelerometer readings for new damper at 5 bar

```
# Accelerometer Data File
# Started @Fri May 11 10:20:20 GMT+05:00 2018
# sensor Vendor: Invensense
# sensor Name: MPU6500 Acceleration Sensor
# sensor Resolution: 0.0011971008m/sec^2; Max Range: 39.2266; Min Delay: 5000
# The sensor's attributes are the result hardware and the Android
capabilities.
# It means that the Android may not utilize all features provided by the
# Some devices and Android versions save battery too much so the device may
go to sleep.
# It just happens after couple of minutes from turning off the scree and it
is easy to find it out.
\# The following file provides the data from accelerometer in the m/s^2
# The diff value is just a time delta between the samples
# data format:
\# so we have 4 columns with values separated by the " "
# X Y Z time from previous sample(ms)
# sensor speed set to:NORMAL
# units set to: m/sec^2
# gravity NOT filtered out
# Accuracy: HIGH
```

Data	Acceleration	Velocity	Displacement
12.247	1.949420905	0.004873552	1.21839E-05
11.481	1.384292957	0.013207837	5.73874E-05
10.36	0.557258455	0.018061715	0.000135561
10.335	0.538814331	0.020801897	0.00023272
9.603	-0.001229608	0.022145859	0.00034009
8.455	-0.848183764	0.020022326	0.00044551
9.21	-0.291171231	0.017173938	0.000538501

9.414	-0.140667183	0.016094342	0.000621671
10.097	0.363226274	0.01665074	0.000703534
9.726	0.08951548	0.017782594	0.000789618
9.455	-0.11041882	0.017730336	0.0008784
9.673	0.050413938	0.017580324	0.000966676
9.588	-0.012296082	0.017675618	0.001054816
8.993	-0.451266224	0.016516713	0.001140297
9.425	-0.132551768	0.015057168	0.001219232
9.414	-0.140667183	0.01437412	0.00129281
9.909	0.224526465	0.014583769	0.001365205
9.425	-0.132551768	0.014813705	0.001438699
8.91	-0.512500715	0.013201074	0.001508735
9.551	-0.039593385	0.011820839	0.00157129
9.606	0.000983687	0.011724315	0.001630153
9.991	0.28502319	0.012439332	0.001690562
9.797	0.141896791	0.013506632	0.001755427
9.92	0.232641879	0.014442978	0.001825301
9.627	0.01647675	0.015065775	0.001899073
9.265	-0.250594159	0.014480481	0.001972939
9.744	0.102795249	0.014110984	0.002044417
9.361	-0.179768725	0.01391855	0.002114491
9.106	-0.367898786	0.012549382	0.002180661

9.446	-0.117058705	0.011336988	0.002240377
10.121	0.380932633	0.011996673	0.002298711
10.171	0.41782088	0.013993557	0.002363687
9.02	-0.431346571	0.013959742	0.00243357
8.959	-0.476350232	0.0116905	0.002497696
9.642	0.027543225	0.010568483	0.002553343
9.097	-0.37453867	0.009700994	0.002604017
9.187	-0.308139825	0.007994298	0.002648255
9.434	-0.125911884	0.006909169	0.002685514
9.416	-0.139191653	0.00624641	0.002718403
9.291	-0.231412271	0.0053199	0.002747318
9.029	-0.424706686	0.003679603	0.002769817
9.815	0.15517656	0.003005777	0.002786531
9.963	0.264365772	0.004054633	0.002804182
9.73	0.09246654	0.004946714	0.002826685
9.373	-0.170915545	0.004750591	0.002850928
9.342	-0.193786259	0.003838837	0.002872402
9.174	-0.317730769	0.002560044	0.002888399
9.646	0.030494284	0.001841953	0.002899404
10.126	0.384621458	0.002879742	0.002911208
9.368	-0.17460437	0.003404785	0.002926919
8.415	-0.877694362	0.000774038	0.002937367

9.888	0.209033401	-0.000897614	0.002937058
9.804	0.147061146	-7.37765E-06	0.002934795
8.789	-0.601770273	-0.00114415	0.002931916
9.648	0.031969814	-0.002568652	0.002922634
9.745	0.103533014	-0.002229895	0.002910638
9.077	-0.389293969	-0.002944297	0.002897702
8.95	-0.482990117	-0.005125007	0.002877529
8.831	-0.570784145	-0.007759443	0.002845318
9.877	0.200917987	-0.008684108	0.002804209
9.405	-0.147307067	-0.008550081	0.002761124
9.075	-0.390769499	-0.009895272	0.00271501
9.853	0.183211628	-0.010414167	0.002664237
9.714	0.080662301	-0.009754482	0.002613815
9.269	-0.2476431	-0.010171934	0.002563999
9.837	0.171407389	-0.010362523	0.002512663
9.691	0.063693707	-0.009774771	0.00246232
9.229	-0.004526104	-0.009626852	0.002413816
9.278	-0.241003215	-0.010240675	0.002364147
8.508	-0.809082222	-0.012865889	0.00230638
8.623	-0.724239254	-0.016699192	0.002232468
8.971	-0.467497053	-0.019678533	0.002141523
7.316	-1.688498036	-0.025068521	0.002029656

8.704	-0.664480293	-0.030950967	0.001889607
10.436	0.61332859	-0.031078846	0.001734533
12.215	1.925812426	-0.024730993	0.001595008
9.781	0.130092552	-0.019591231	0.001484202
9.917	0.230428584	-0.018689928	0.001388499
8.256	-0.994998988	-0.020601354	0.001290271
8.305	-0.958848506	-0.025485973	0.001175053
10.552	0.698909324	-0.026135821	0.001045998
12.253	1.953847494	-0.019503929	0.000931899
11.702	1.54733901	-0.010750962	0.000856262
8.221	-1.020820761	-0.009434667	0.000805798
9.823	0.16107868	-0.011584022	0.000753251
10.107	0.370603924	-0.010254815	0.000698654
10.289	0.504877144	-0.008066113	0.000652852
8.947	-0.485203412	-0.008016928	0.000612644
9.585	-0.014509377	-0.00926621	0.000569436
9.054	-0.406262563	-0.01031814	0.000520475
10.222	0.455446892	-0.010195179	0.000469192
9.484	-0.089023637	-0.009279121	0.000420506
8.75	-0.630543106	-0.011078038	0.000369613
10.924	0.973357883	-0.010221001	0.000316366
9.196	-0.301499941	-0.008541356	0.00026946

13.569	2.924746161	-0.001983241	0.000243148
11.587	1.462496041	0.008984865	0.000260652
12.032	1.790801442	0.017118108	0.00032591
9.139	-0.343552542	0.020736231	0.000420546
8.76	-0.623165456	0.018319436	0.000518185
7.827	-1.311500149	0.013482772	0.00059769
8.243	-1.004589933	0.007692546	0.000650629
7.207	-1.768914415	0.000758786	0.000671757
7.848	-1.296007086	-0.006903518	0.000656395
11.246	1.210918195	-0.00711624	0.000621346
10.972	1.008770601	-0.001567018	0.000599638
16.818	5.321744465	0.014259269	0.000631368
11.101	1.103942278	0.030323486	0.000742825
6.72	-2.128205943	0.027762827	0.000888041
9.029	-0.424706686	0.021380545	0.001010899
7.28	-1.715057574	0.016031135	0.001104429
11.07	1.081071565	0.01444617	0.001180622
12.342	2.019508574	0.02219762	0.001272231
10.469	0.637674834	0.028840579	0.001399827
6.161	-2.540616547	0.024083224	0.001532136
7.375	-1.644969904	0.013619258	0.001626393
10.942	0.986637652	0.011973427	0.001690374
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8.391	-0.895400721	0.01220152	0.001750812
9.787	0.134519142	0.010299316	0.001807064
10.502	0.662021077	0.012290666	0.001863539
8.313	-0.952946386	0.011563353	0.001923174
6.72	-2.128205943	0.003860472	0.001961733
9.012	-0.43724869	-0.002553164	0.001965002
8.798	-0.595130388	-0.005134112	0.001945783
13.417	2.812605889	0.000409577	0.001933972
10.714	0.818427245	0.00948716	0.001958714
8.919	-0.50586083	0.010268576	0.002008103
8.477	-0.831952936	0.006924041	0.002051085
8.661	0.696204186	0.003103648	0.002076154

<sup>#</sup> Completed @Fri May 11 10:21:22 GMT+05:00 2018